EVALUATION OF SAR DATA AS SOURCE OF GROUND CONTROL INFORMATION: FIRST RESULTS

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ABSTRACT:

The high resolution imaging modes of modern SAR sensors has made SAR data compatible with optical images. SAR data offers various capabilities which can enhance the geometric correction process of optical images (accurate, direct and ground-independent georeferencing capabilities and global DEM products). In this paper the first results of an on-going study on the evaluation of SAR data as source of ground control information for the georeferencing of optical images are presented. The georeferencing of optical images using SAR data is in fact a co-registration problem which involves multimodal, multiemporal, and multiresolution data. And although 2D transformations have proved to be insufficient for the georeferencing process, as they can not account for the distortions due to terrain, quite a few approaches on the registration of optical to SAR data using 2D-2D transformations can still be found in the literature. In this paper the performance of 2D-2D transformations is compared to the 3D-2D projective transformation over a greater area of Earth's surface with arbitrary terrain type. Two alternative forms of ground control information accuracy specification of the optical image, as well as to the accuracy of exhaustive georeferencing done by third parties.

1 INTRODUCTION

State-of-the-art SAR sensors offer high resolution images which are comparable with high resolution optical images. They offer accurate, direct and ground-independent georeferencing capabilities and global DEM products. These capabilities combined can theoretically provide Ground Control Information (GCI) for the georeferencing of optical images. The idea of collecting GCI from air or space is quite attractive as it enhances the 'remote sensing' nature of optical images, making them independent of ground surveys which are usually necessary for the collection of the GCI. It is useful both for cases where direct georeferencing of optical images is not available and for cases where the direct georeferencing is not accurate enough.

In order to be able to extract GCI from SAR data and use it for real world operational cases, it is necessary that the SAR and optical images have also comparable accuracy. Currently, the geolocation accuracy specification defined by the operators of the sensors, as well as the pixel size of optical and SAR images, imply that the accuracy is indeed comparable. However, various results in the literature show that this is quite an unclear issue, which demands further research and experimentation:

1) The identification of points, the common form of GCI, is still quite ambiguous on SAR images, due to their speckled nature, slant range geometry and radiometric properties. Furthermore it is hard to guarantee that in real world practical cases, the existing methods will succeed to extract the same points on optical and on SAR images. As it is often reported in the literature, the accurate identification of homologous points on optical and SAR images is hard even for the human eye perception in real world images. This ambiguity is gradually faced using feature-based matching of more complex features ((Dare and Dowman, 2001), (Karjalainen, 2007), (Hong and Schowengerdt, 2005), (Vassilaki, 2012a)) which can be identified more reliably on optical and SAR images than the points.

2) Accuracy results on the co-registration of optical and SAR

data vary. (Dare and Dowman, 2001) reported co-registration accuracy of 1.5 pixel for low terrain height variations, (Hong and Schowengerdt, 2005) reported co-registration accuracy of 0.6-3 pixels for reasonably flat terrain, (Vassilaki et al., 2009b) reported 1 pixel for small image patches over hilly terrain. (Reinartz et al., 2011) reported co-registration accuracy of 2-6 pixels for the co-registration of a satellite optical image to a geometrically corrected satellite SAR image over urban areas with moderate terrain. (Vassilaki, 2012a) reported roughly the same accuracy as (Reinartz et al., 2011) for the co-registration of a whole satellite slant range SAR image to an orthorectified aerial optical image, on mountain terrain with direct georeferencing (Vassilaki et al., 2011).

Accuracy results reported in literature should not be interpreted comparatively, as different methods, data sets, terrain and land use, under different objectives were processed. The only safe conclusion is that the state-of-the-art methods achieve roughly 1 pixel accuracy for the co-registration of small patches of data, which are geometrically corrected, or/and over flat areas. However, the accuracy of co-registration of real world, not geometrically corrected, data over greater areas of Earth's surface with arbitrary terrain type (not necessarily flat) remains an open issue.

This paper contributes to this research framework by presenting the first results of an on going study on the evaluation of SAR data as source of GCI. In the following sections, the general objectives of the study are presented, as well as the specific objectives of the current paper, the test site and the data sets, and the methods and the tools which are used. The first results of the study are presented and discussed.

2 TEST SITE AND DATA SETS

The test site is JRC's Maussane Terrestrial Test Site which is located near Maussane-les-Alpilles in South France. The area exhibits numerous land uses (forest areas, olive groves, small urban areas, water bodies) and terrain variations (mountains, plains and

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water bodies). The area used in this paper spans $4^{\circ} 40'$ to $4^{\circ} 50'$ E and $43^{\circ} 39'$ to $43^{\circ} 46'$ N (Figure 1(a)) and is about 100 Km².

The SAR data over Maussane test site was collected in 2009 and consists of orthorectified aerial SAR images (Figure 1(b)), DSM (Figure 1(c)) and DTM which were interferometrically produced, and the 3D road network (Figure 1(b)) which was extracted by the orthorectified SAR images and the DSM/DTM ((Mercer, 2007), (Zhang et al., 2010), www.intermap.com). The orthorectified SAR images have 1.25 m pixel size and according to the general accuracy specifications their horizontal absolute accuracy is 4 m (CE90%). The DSM/DTM are posted at 5 m and according to the general accuracy specifications the vertical accuracy is < 1m (LE90%) for the 40% of the coverage area, 1–3 m (LE90%) for the 40% of the coverage area and > 3 m (LE90%) for the rest 20% of the coverage area. The planar geometry of roads' centrelines was extracted from the orthorectified SAR images and the elevation of the centrelines was determined from the interferometrically produced DTM/DSM. The accuracy of the 3D road network meets the accuracy of the initial SAR data. The planar coordinates (geographic latitude/longitude) are available in the horizontal geodetic datum ETRS89 (European Terrestrial Reference System 1989). The orthometric elevation is provided in the EGG07 (European Gravimetric Geoid model 2007) vertical geoid model.

The optical image was collected in 2010 and it is a level 2A standard satellite imagery. The nominal spatial resolution of the panchromatic imaging mode is 50 cm, and 2 m for the multispectral (8 spectral bands) imaging mode (http://www.digitalglobe.com). The general geolocation accuracy specification of the optical image is 6.5m (CE90%), with predicted performance in the range of 4.6 to 10.7 m (CE90%), excluding terrain and off-nadir effects. The geolocation accuracy specification of the optical image GCPs is 2.0 m CE90% (http://www.digitalglobe.com). The off-nadir view angle is 36° , the cross-track view angle is 34.7° and the in-track view angle is -10.4° for the specific image used in this paper (Nowak Da Costa and Walczynska, 2011).

3 OVERVIEW AND OBJECTIVE

The general objectives of the study are: 1) to contribute to the evaluation of SAR data as source of GCI for the georeferencing of optical images and 2) to benchmark the performance of two alternatives forms of GCI: Ground Control Linear Features (GCLFs) and Ground Control Points (GCPs). The accuracy of the georeferencing (either using GCLFs or GCPs) is computed using manually collected independent check points (CPs). The accuracy of the georeferencing is compared to the geolocation accuracy specification of the optical image, as well as to the accuracy of the exhaustive georeferencing done by third parties. The test area is the well-known JRC's Maussane test site near Mausanne-les-Alpilles in France.

The georeferencing process establishes the relationship of the 2D image space with the 3D object space. 3D-2D projection transformation models (empirical or physical) are used for this purpose (Toutin, 2004), (Dowman et al., 2012). Although literature abounds with fully justified conclusions on the general unsuitability of 2D-2D projective transformations for the georeferencing process, 2D-2D transformations (even simple 2D rigid and affine ones) are still used for the development of methods for the corregistration of optical and SAR images. Arbitrary assumptions such as of flat terrain, small image patches and geometrically corrected images, enable such methods to compute good results.

The objective of this paper is to test the performance of the 2D-2D projective transformations applied to the georeferencing of a



(a) Test site and coverage of the satellite optical image(in red) and the aerial SAR data (in cyan)



(b) 3D roads centrelines overlaid on the orthorectified SAR image



(c) The interferometrically produced DSM

Figure 1: Test site and data sets.

level 2A satellite optical image using SAR data (in other words the co-registration of optical and SAR data), over greater areas of Earth's surface (not just small image patches), with terrain of arbitrary form (not necessarily flat). Two different transformation models are used in this paper: 1) 2D-2D and 2) 3D-2D 1st order polynomial functions (PFs). Two different forms of GCI are used: 1) GCPs and 2) GCLFs.

4 METHOD

The significance of using GCI for the geometric correction of optical images has been noted, analyzed, researched and discussed exhaustively in the related literature. The most common form of GCI is the point, the fundamental feature of all photogrammetric processes. Numerous methods, data sets and tests have been presented over the years using GCPs ((Toutin, 2004), (Dowman et al., 2012). Repetition of this long-term research and practical knowledge would be redundant.

More complex features, such as straight lines and free form linear features can be exploited as an alternative/complementary form of GCI. The use of these features is not common (research is still in progress and the only software available is in-house developed research software). In this paper, the use of GCLFs is based on the matching method introduced in (Vassilaki et al., 2008). The iterative closest point (ICP) algorithm ((Besl and McKay, 1992), (Zhang, 1994)) is used for accurate and robust global matching of heterogeneous FFLFs. The method matches 2D heterogeneous FFLFs with a rigid transformation. It was further expanded in order to match FFLFs of different dimensionality (3D-2D) with non-rigid projective transformation and it is fully documented in (Vassilaki et al., 2012b). For efficiency convenience and user friendliness the method has been incorporated into ThanCAD (Stamos, 2007), an open-source CAD (http://sourceforge.net/projects/thancad/).

The matching of two FFLFs of the same dimensionality (2D-2D, 3D-3D) is done by an iterative process of determining closest point pairs between the two FFLFS and then using them to compute the transformation parameters by least squares adjustment (LSA). Closest point pairs are computed by splitting a FFLF to a large set of consecutive interpolated points, each one very close to its previous and its next point. Then, the distances of all these points to a node of the other FFLF are computed; the closest points between the two FFLFs are the points with the smallest distances. This process may be computationally expensive but it is doable with modern computers, and it is relatively easy to speed it up with a divide-and-conquer approach. Further acceleration can be achieved by parallel computing (Stamos et al., 2009). In the case of FFLFs of different dimensionality (3D-2D) the 3D nodes of the 3D FFLF are projected to the 2D image space using an initial or previous approximation of the transformation parameters, saving the association of each 3D node and its 2D projection. The closest points computed as in the 2D-2D case, are converted to 3D-2D pairs through the saved association, and they are used to compute the projection parameters by LSA.

The ICP algorithm needs a good initial approximation to converge, which means that the two FFLFs must be close enough to each other. Automatic pre-alignment is done using the rigid similarity transformation computed exploiting physical properties of the two FFLFs, or using the non-rigid first order polynomial (affine) transformation computed exploiting characteristic statistical properties of the FFLFs (Vassilaki et al., 2012b).

In the case of networks of FFLFs of the same dimensionality (2D-2D, 3D-3D) or different dimensionality (3D-2D), the correspondences of FFLFs must be established. Assuming that the

two data sets are initially pre-aligned, a FFLF of the first data set corresponds to the FFLF of the other data set which is 'closest' to it. However, the definition of 'closest' is ambiguous for a FFLF which may span many other FFLFs. Different nodes of the same FFLF may be closest to nodes of different FFLFs. (Vassilaki et al., 2009a) introduced the term 'distance' as an integral measure of how far or how different two FFLFs are. The pair of FFLFs which have the smallest 'distance' are assumed to correspond to each other. Four candidates for the 'distance' measure were suggested: the Euclidean distance between characteristic homologous points, namely the first nodes (d1), the last nodes (dN), or the centroids (d), and the absolute difference of the FFLFs lengths (S). For robustness, the biggest of these four values can be used as the 'distance' of the FFLFs. In the very unlikely case that the 'distance' is ambiguous (almost the same) for two or more pairs of FFLFs, application of the full ICP can be used to determine which FFLFs correspond to each other. ICP is the best and more robust approach, but it is very time consuming and should be avoided if possible. The method proceeds with an ICP step, it brings the FFLFs even closer and it then reevaluates the correspondence, as the "distance" between any pair of FFLFs is obviously changed. Furthermore, ICP automatically rejects two unrelated FFLFs marked to correspond if they do not overlap (Vassilaki, 2012a).

All the FFLFs of a network share a common transformation. In order to compute the common transformation, LSA is applied to all the pairs of FFLFs simultaneously. The equations produced by the homologous points of all pairs of FFLFs are assembled into the same LSA matrices. The LSA computes the transformation which best fits all the pairs of FFLFs. The computed transformation brings the FFLFs closer together, and thus the correspondences are re-evaluated, in case that the previous, poorer, transformation led to a few false correspondences. Since all pairs of FFLFs share the same transformation, a good approximation of the transformation of a single pair of FFLFs, automatically computed ((Vassilaki, 2012a), can be used to bring the data sets close together, essentially prealigning them.

5 APPLICATION AND RESULTS

5.1 Measurement of the GCI

160 common points were identified between the optical and the SAR image. They were measured in the 2D optical image space (pixels) and in the 3D object space (meters) of the SAR image. The elevation of the points measured on the SAR image was interpolated from the available interferometrically produced DEM (DSM). Some of the points were used as GCPs in order to compute the transformation models, and the remainder of the points were used as CPs in order to evaluate the computation. As the optical and the SAR image were unitemporal and the SAR image was orthorectified, it was not very hard to identify common regions and characteristics. On the other hand, the fuzzy and speckled nature of the SAR image made the identification and measurement of single points ambiguous. The computation of the transformation model (Section 5.2) and its application to project 3D points to the optical image, revealed a few gross errors and point ambiguities, which either could not be resolved and thus new points were measured, or led to re-measurement of the picked points. The procedure was then iterated many times. In general the measurement of the common points between the optical and the SAR image was a very laborious process.

Additionally 23 FFLFs were identified between the optical and the SAR image. The SAR data was accompanied by the vectors

of the centrelines of the roads (3D Road Vectors) (Zhang et al., 2010) and thus no extraction of roads was necessary on the SAR data (Figure 1(b)). Common roads between the SAR data and the optical image were identified and then the edges of the roads were extracted manually on the optical image. The centrelines of the roads on the optical image space were computed with skeletonization techniques. Although it was possible to identify a multitude of common roads between the optical and the SAR image, just a few of them were sufficient to ensure full GCI coverage of the optical image. The road centrelines were then used as matching primitives. The FFLFs with known 2D optical image space coordinates and known 3D object space node coordinates (readily available from the orthorectified SAR image and the DEM) were then used as GCLFs in order to compute the transformation model. Some editing (mostly merging) was needed to group the 3D roads according to the 2D roads. In general the measurement of common FFLFs was a straightforward and swift process.

5.2 Computation of the georeferencing

For both forms of GCI, 2D-2D and 3D-2D transformation models were used to georeference the optical image. The transformation models used are the following 1st order polynomial functions (PFs):

- the 2D-2D 1st order PFs

$$x = a_1 X + a_2 Y + a_3 y = b_1 X + b_2 Y + b_3$$
 (1)

- the 3D-2D 1st order PFs

$$x = a_1 X + a_2 Y + a_3 Z + a_4 y = b_1 X + b_2 Y + b_3 Z + b_4$$
 (2)

Four combinations of GCI and transformation models were used for the computation of the georeferencing of the optical image:

- 1) 2D-2D PFs and GCPs
- 2) 2D-2D PFs and GCLFs
- 3) 3D-2D PFs and GCPs
- 4) 3D-2D PFs and GCLFs

In the first and the third case 11 points which span the optical image were used as GCPs (Figure 2) for the computation of the correspondent transformation model. In the second and the fourth case 23 FFLFs which span the optical image were used as GCLFs (Figure 2) for the computation of the correspondent transformation model. As a byproduct of the georeferencing process, the 23 GCLFS also produced automatically 91788 common 3D-2D points between the two data sets (2D optical image space and 3D object space of the SAR image). These points can be exploited by any standard photogrammetric/remote sensing software which does not have GCLFs capabilities.

5.3 Evaluation

The RMSE of the four cases was computed using manually collected independent CPs. From the 160 common points between the optical and the SAR image (Section 5.1), 11 points were used as GCPs (Section 5.2) and the remaining 149 points (in green in Figure 2) were used as CPs. The RMSE is shown in Table 1. The accuracy of the four cases was evaluated using:

 the geolocation accuracy specification of the optical image which is 6.5 m (CE90%), with predicted performance in the range of 4.6 to 10.7 m (CE90%), excluding terrain and off-nadir effects.
the geolocation accuracy specification of the optical image with registration to GCPs which is 2.0 m (CE90%).

3) the accuracy computed independently by JRC using GCPs and CPs measured with GPS ((Nowak Da Costa and Walczynska,







(b) GCLFs and CPs

Figure 2: The distribution of the GCPs (in blue), the GCLFs (in blue) and the CPs (in green) over the test site.

2011)) and exhaustive testing of mathematical models as implemented in numerous standard software. The computed accuracy (Table 1) shows that:

1) The 2D-2D transformations lead to far worse accuracy (several tens of meters) than the geolocation accuracy specification defined by the operator of the sensor (6.5 m), for both forms of GCI (GCPs and GCLFs). Furthermore, since a level 2A satellite optical image was used in this paper, the accuracy is expected to be even worse in the case of basic imagery products (for instance level 1A). Thus the 2D transformations should be abandoned for real world practical cases over greater areas of Earth's surface with arbitrary terrain.

2) The two forms of GCI (GCPs and GCLFs) used in this paper lead to the same accuracy (3.5 m), probably because it reflects the accuracy of the CPs themselves, namely 4 m planar and 1-2m vertical accuracy. However, it should be noted that the mea-

Model	GCI	X (m)	Y(m)	Planar (m)
2D-2D PFs	GCPs	32.3	14.6	35.4
	GCLFs	37.8	35.0	51.5
3D-2D PFs	GCPs	2.5	2.7	3.7
	GCLFs	2.5	2.4	3.5

Table 1: The CPs RMSE using 1st order 2D-2D and 3D-2D PFs for the two different forms of GCI (GCPs and GCLFs).

surement of the common points between the optical and the SAR image was a laborious process and thus the georeferencing using GCLFs is considered superior. 3) The computed accuracy (3.5 m) does not (and can not) meet the geolocation accuracy specification with registration to GCPs (2 m). More accurate GCI (for example measured with GPS) should be used for this purpose (Nowak Da Costa and Walczynska, 2011). However, the computed accuracy (3.5 m) is better than the geolocation accuracy specification without GCPs (6.5, with predicted performance in the range of 4.6 to 10.7 m), more so because the geolocation accuracy specification does not include terrain and off-nadir effects, while the test region and data include both effects.

6 CONCLUSION

In this paper the first results of an on-going study on the evaluation of SAR data as source of GCI, under realistic conditions, were presented. More specifically GCPs and GCLFs were collected from orthorectified SAR images and the corresponding interferometrically produced DEM. They were used to compute the georeferencing of a level 2A satellite optical image over a greater areas of Earth's surface (not just a small patch), with arbitrary terrain type (not necessarily flat). Both 2D-2D and 3D-2D transformation models were used and the accuracy was evaluated using independent CPs. The accuracy of the 2D-2D models was unacceptable to the point that they should not be used at all. The accuracy of the 3D-2D models reached the accuracy of the CPs themselves, which suggests that more accurate GCI will probably lead to better accuracy, and that SAR data has compatible accuracy with optical images. Further research and experimentation on the subject is thus encouraged.

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