AN EFFICIENT INITIALIZATION METHOD FOR K-MEANS CLUSTERING OF HYPERSPECTRAL DATA

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ABSTRACT:

K-means is definitely the most frequently used partitional clustering algorithm in the remote sensing community. Unfortunately due to its gradient decent nature, this algorithm is highly sensitive to the initial placement of cluster centers. This problem deteriorates for the high-dimensional data such as hyperspectral remotely sensed imagery. To tackle this problem, in this paper, the spectral signatures of the endmembers in the image scene are extracted and used as the initial positions of the cluster centers. For this purpose, in the first step, A Neyman–Pearson detection theory based eigen-thresholding method (i.e., the HFC method) has been employed to estimate the number of endmembers in the image. Afterwards, the spectral signatures of the endmembers are obtained using the Minimum Volume Enclosing Simplex (MVES) algorithm. Eventually, these spectral signatures are used to initialize the k-means clustering algorithm. The proposed method is implemented on a hyperspectral dataset acquired by ROSIS sensor with 103 spectral bands over the Pavia University campus, Italy. For comparative evaluation, two other commonly used initialization methods (i.e., Bradley & Fayyad (BF) and Random methods) are implemented and compared. The confusion matrix, overall accuracy and Kappa coefficient are employed to assess the methods' performance. The evaluations demonstrate that the proposed solution outperforms the other initialization methods and can be applied for unsupervised classification of hyperspectral imagery for landcover mapping.

1. INTRODUCTION

Classification can be categorized into two main groups of supervised and unsupervised classification methods. Although supervised methods lead to the better results, unsupervised or clustering techniques have been attracted a lot of attentions because they don't need any training data and procedure (Melgani and Pasolli, 2013).

Among different clustering algorithms, partitional methods are one of the best techniques for high-dimensional data, e.g., hyperspectral data. This is mainly because they have lower complexity (Celebi et al., 2013). The k-means algorithm is undoubtedly the most widely used partitional clustering algorithm (Jain, 2010). However, k-means has two significant disadvantages. First, it is sensitive to the outlier and noise. Second, it is highly sensitive to the selection of the initial clusters. Adverse effects of improper initialization include empty clusters, slower convergence, and a higher chance of getting stuck in bad local minima. Fortunately, these two drawbacks can be alleviated using an appropriate initialization method (Celebi et al., 2013).

The problem of the initialization can be addressed by either deterministic (Celebi et al., 2013) or heuristic methods (Abraham et al., 2008). Although heuristic methods like particle swarm optimization (PSO) may lead to the best results, they are time-consuming and may have less stability in high-dimensional data. Accordingly, deterministic methods have priority if they lead to an acceptable result.

To address the initialization problem, different methods have been proposed especially for hyperspectral imagery. In (Sun et al., 2013), an artificial bee colony algorithm is used to find the appropriate position of cluster centers in hyperspectral data. In another similar work, (Namin et al., 2013) used the PSO clustering algorithm in Minimum noise fraction space. The comparison of their results with the K-means clustering method

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showed better performance for the PSO clustering in minimum noise fraction feature space. In (Celebi et al., 2013), the authors compared different initialization methods for k-means. Although, they have shown Bradley and Fayyad's method is one of the best initialization methods, it was also demonstrated that the popular initialization methods often perform poorly and that there are in fact strong alternatives to these methods.

In this paper, a new initialization method for hyperspectral data clustering using k-means has been proposed. In this method, first, the number of endmembers is estimated by using the HFC (Harsanyi et al., 1993) technique. Then the spectral signature of endmembers (i.e., initial position of cluster centers) is obtained based on the MVES method.

The rest of the paper is organized as follows. Section 2 presents a summary of k-means, HFC and MVES algorithms. Section 3 introduces our proposed method. Section 4 describes the experimental setup and results. Lastly, section 5 gives our conclusion.

2. THEORETICAL BACKGROUND

2.1 K-Means Clustering

K-means clustering (MacQueen, 1967) is a method commonly used to automatically partition a dataset into K groups. It proceeds by selecting K initial cluster centers and then iteratively refining them as follows. 1) First, each point is assigned to its closest cluster center, 2) Each cluster center Cj is updated to be the mean of its constituent points (Wagstaff et al., 2001). From the mathematical perspective, given a data set $X = \{x_1, x_2, ..., x_N\}$ in \mathbb{R}^D , i.e. N points (vectors) each with D attributes (components), K-means algorithm divides X into K exhaustive and mutually exclusive clusters $P = \{p_1, p_2, ..., p_K\}$,

 $\bigcup_{i=1}^{K} p_i = X$, $p_i \cap p_j = \emptyset$ for $1 \le i \ne j \le K$. This algorithm generates clusters by optimizing a criterion function. The most intuitive and frequently used criterion function is the Sum of Squared Error (SSE) given by:

SSE =
$$\sum_{i=1}^{K} \sum_{x_j \in p_i} ||x_j - c_i||_2^2$$
 (1)

Where $\|.\|_2$ denotes the Euclidean (\mathcal{L}_2) norm and $c_i = \frac{1}{|p_i|} \sum_{x_j \in p_i} x_j$ is the centroid of cluster p_i whose cardinality is $|p_i|$. The optimization of (1) is often referred to as the minimum SSE clustering (MSSC) problem (Celebi et al., 2013). Based on application, different similarity measures can be used instead of Euclidean distance (ED). In this study, Spectral similarity value (SSV) (Farifteh et al., 2007), as one of the most successful similarity measures in hyperspectral data (Homayouni and Roux, 2004), is used. SSV combines brightness and shape similarity. It is a combined measure of Pearson correlation (PC) and ED measures.

2.2 HFC Method

A Neyman–Pearson detection theory-based eigen-thresholding method, referred to as the HFC method, was developed to determine the number of endmembers, which called Virtual Dimensionality (VD), in AVIRIS data (Harsanyi et al., 1993). It first calculated the sample correlation matrix $\mathbf{R}_{L\times L}$ and sample covariance matrix $\mathbf{K}_{L\times L}$ and then found the difference between their corresponding eigenvalues, where L is the number of spectral band in the image. Let $\{\lambda_1 \geq \lambda_2 \geq ... \geq \lambda_L\}$ and $\{\lambda_1 \geq \lambda_2 \geq ... \geq \lambda_L\}$ be two sets of eigenvalues generated by $\mathbf{R}_{L\times L}$ and $\mathbf{K}_{L\times L}$, called correlation eigenvalues and covariance eigenvalues, respectively. By assuming that signal sources are nonrandom unknown positive constants and noise is white with zero mean, we can expect that:

and

$$\lambda'_{i} = \lambda_{i}, \quad \text{for } i = VD + 1, \cdots, L$$
 (3)

More specifically, the eigenvalues in the ith spectral channel can be related by

 $\lambda'_i > \lambda_i$, for $i = 1, \dots, VD$

$$\lambda'_i > \lambda_i > \sigma_{n_i}^2$$
, for $i = 1, \dots, VD$ (4)

and

$$\lambda'_{i} = \lambda_{i} = \sigma_{n_{i}}^{2}, \quad \text{for } i = VD + 1, \cdots, L \tag{5}$$

Where σ^2_{ni} is the noise variance in the ith spectral channel (Chein and Qian, 2004). In order to determine the VD, Harsanyi et al formulated the problem of determination of VD as a binary hypothesis problem as follows:

$$\begin{split} H_0: z_i = \lambda_i - \lambda_i = 0, \quad \text{versus} \quad H_1: z_i = \lambda_i - \lambda_i > 0, \\ \text{for} \quad i = 1, 2, \cdots, L \end{split} \tag{6}$$

Where, the null hypothesis H_0 represents the case that the correlation eigenvalue is equal to its corresponding covariance eigenvalue. The alternative hypothesis H_1 is for the case that the correlation eigenvalue is greater than its corresponding covariance eigenvalue. In other words, when H_1 is true (i.e., H_0 fails), it implies that there is an endmember contributing to the correlation eigenvalue in addition to noise, since the noise energy represented by the eigenvalue of **R** L×L in that particular

component is the same as the one represented by the eigenvalue of $K_{\ L\times L}$ in its corresponding component.

Despite the fact that the λ_i and λ'_i are unknown constants, we can model each pair of eigenvalues λ'_i and λ_i under hypothesis H₀ and H₁ as random variables by the asymptotic conditional probability densities given by

$$p_0(z_i) = p(z_i \left| H_0 \right) \cong N(0, \sigma_{z_i}^2), \quad \text{ for } i = 1, 2, \cdots, L \quad (7)$$

and

$$p_1(z_i) = p(z_i | H_1) \cong N(\mu_i, \sigma_{z_i}^2), \text{ for } i = 1, 2, \cdots, L$$
 (8)

respectively, where μ_i is an unknown constant and the variance $\sigma^2{}_{zi}$ is given by

$$\sigma^{2}_{zi} = \operatorname{Var}[\lambda_{i} - \lambda_{i}] = \operatorname{Var}[\lambda_{i}] + \operatorname{Var}[\lambda_{i}] - 2\operatorname{Cov}(\lambda_{i}, \lambda_{i})$$
for i= 1, 2, ..., L.
(9)

Eventually, they defined the false-alarm probability and detection power (i.e., detection probability) by using above mentioned equations and some approximations as follow:

$$P_{F} = \int_{\tau_{i}}^{\infty} p_{0}(z) dz$$
(10)
$$P_{D} = \int_{\tau_{i}}^{\infty} p_{1}(z) dz$$
(11)

A Neyman–Pearson detector for $\lambda_i - \lambda_i$, denoted by $\delta_{NP}(\lambda_i - \lambda_i)$, in the binary composite hypothesis testing problem can be obtained by maximizing the detection power P_D in (11), while the false-alarm probability P_D in (10) is fixed at a specific given value, α , which determines the threshold value τ_i in (10) and (11). So, a case of $\lambda_i - \lambda_i > \tau_i$ indicating that $\delta_{NP}(\lambda_i - \lambda_i)$ fails the test, in which case there is signal energy assumed to contribute to the eigenvalue λ_i in the ith data dimension. It should be noted that the test for hypothesis must be performed for each of L data dimensions. Therefore, for each pair of $\lambda_i - \lambda_i$, the threshold τ is different and should be i-dependent, i.e., τ_i (Chein and Qian, 2004).

2.3 MVES Algorithm

(2)

Minimum Volume Enclosing Simplex (MVES) is an unmixing algorithm without requiring the pure-pixel assumption, which estimates the endmembers by vertices of a minimum-volume simplex enclosing all the observed pixels.

Linear mixture model is a widely used approach for spectral unmixing of remotely sensed hyperspectral imagery. Let **M** be an L×P endmember signature matrix denoted by $[\mathbf{m}_1, \dots, \mathbf{m}_P]$, where \mathbf{m}_i is an L×1 column vector represented by the signature of the ith material resident in the image scene, and P is the number of materials in the image scene. In linear mixture model, spectral signature of a pixel vector $\mathbf{r} = (\mathbf{r}_1, \mathbf{r}_2, \dots, \mathbf{r}_L)^T$ can be represented by a linear regression model as follows:

$$\mathbf{r} = \sum_{i=1}^{P} \mathbf{a}_i \mathbf{m}_i + \mathbf{n} = \mathbf{M}\mathbf{a} + \mathbf{n}$$
(12)

In the equation above, $\mathbf{a} = (a_1, a_2, ..., a_P)^T$ is a P×1 column abundance vector associated with \mathbf{r} , and $\mathbf{n} = (n_1, n_2, ..., n_L)^T$ is noise or can be interpreted as a measurement error (Heinz and Chein, 2001). The final goal of a spectral unmixing method is to recover the matrix \mathbf{M} and the endmember fractional abundance \mathbf{a} for each observed pixel. To do so, usually, noise needs to be minimized (in least squares fashion), and the volume of the simplex spanned by the columns of matrix \mathbf{M} should be minimized (Winter, 1999). In MVES algorithm, Craig's unmixing criterion (Craig, 1994) was employed to formulate the hyperspectral unmixing as an MVES optimization problem.

The key property of this method is that all the dimension-reduced pixels \mathbf{r}_i for i = 1, ..., N, must be inside the simplex constructed by the dimension-reduced endmembers α_i for i=1, ..., P. This concept is illustrated in figure 1.



Figure 1. Scatter plot of two-dimensional dimension-reduced pixels illustrating the MVES problem for hyperspectral unmixing (Chan et al., 2009)

This figure also demonstrates that dimension-reduced pixels \mathbf{r}_i can also be enclosed by a different simplex, denoted by conv{ $\beta_1, ..., \beta_P$ }. Nevertheless, by intuitive grounds, one would expect that the data enclosing simplex with the minimum volume should coincide with the true endmember simplex conv{ $\alpha_1, ..., \alpha_P$ }. This is exactly the belief of Craig's unmixing criterion (Craig, 1994). The problem of finding the MVES can be formulated as an optimization problem as follows (Chan et al., 2009):

$$\min_{\beta_1,\dots,\beta_P} V(\beta_1,\dots,\beta_P)$$
s.t. $\mathbf{r}_i \in \operatorname{conv}\{\beta_1,\dots,\beta_P\}, \forall i$
(13)

Where $V(\beta_1, ..., \beta_P)$ is the volume of the simplex conv{ $\beta_1, ..., \beta_P$ } $\subset \mathbb{R}^{P-1}$ given by

$$V(\beta_1, \dots, \beta_P) = \frac{\left|\det\left(\Delta(\beta_1, \dots, \beta_P)\right)\right|}{(P-1)!}$$
(14)

Where

$$\Delta(\beta_1, \dots, \beta_P) = \begin{bmatrix} \beta_1 & \dots & \beta_P \\ 1 & \dots & 1 \end{bmatrix}$$
(15)

Where $\Delta(\beta_1, ..., \beta_P)$ is always a square matrix, since the dimension-reduced pixels and endmembers are in a p-1 dimensional space.

A cyclic minimization algorithm for approximating the MVES problem was developed using linear programs (LPs), which can be practically implemented by readily available LP solvers (Chan et al., 2009).

3. PROPOSED METHODS

In order to clustering of hyperspectral data, in this study, a multistep framework was presented to resolve the problem of initialization of k-means and improve the clustering efficiency. The stages of this proposed method, namely, MVES initialization method has been illustrated in figure 2.



Figure 2. MVES Initialization method

4. DISCUSSION AND RESULTS

4.1 Dataset

Experiments are performed using the Pavia University data set. This data set was acquired by the ROSIS sensor during a flight campaign in 2003 over the campus of Pavia University in the north of Italy. This data contains 610 by 340 pixels with 103 spectral bands. The geometric resolution is 1.3 m. nine ground-truth classes were considered in the experiments: Trees, Gravel, Meadows, Asphalt, Metal sheets, Bricks, Bitumen, Shadows and Bare soil. Figure 3 shows the ground-truth map and a color composite image of this data set.



To reduce the effects of spectral bands with higher radiance values on those having lower values, the data is linearly normalized in the range of [0, 1]. Furthermore, before using this data sets, its background is ignored. This is because no information is available about these areas.

4.2 Experimental results

In this study, the proposed initialization method for k-means clustering of hyperspectral data is compared with two of most frequently used methods, i.e. Bradley &. Fayyad (BF) and random methods. In the first step of the new method, the number of endmembers is estimated by HFC algorithm as 9. The false alarm probability for this detection problem is set to 0.001. As it is said earlier, among different similarity measures for k-means clustering, SSV is used here in all three cases.

In the first case, initial position of cluster centers are obtained using Bradley &. Fayyad (BF) method (Bradley and Fayyad, 1998). According to (Celebi et al., 2013), this method is one of the best methods for k-means initialization in different datasets, and as a result, it is used here to be compared with our proposed method. BF method starts by randomly partitioning of the dataset into J=10 subsets. Clustering results of this case are tabulated in table 1.

		Classified											uo
		Bricks	Bitumen	Trees	Gravel	Asphalt	Shadows	Metal Sheets	Meadows	Bare Soil	Total	PA	Omissi
Ground Truth	Bricks	3555	97	0	0	0	0	0	16	14	3682	96.6	3.4
	Bitumen	97	1233	0	0	0	0	0	0	0	1330	92.7	7.3
	Trees	0	0	1798	1145	4	1	1	19	96	3064	58.7	41.3
	Gravel	1682	414	0	0	0	0	0	1	2	2099	0.0	100.0
	Asphalt	666	5893	0	0	1	2	33	12	24	6631	0.0	100.0
	Shadows	0	1	0	0	0	946	0	0	0	947	99.9	0.1
	Metal Sheets	13	3	0	0	513	0	815	0	1	1345	60.6	39.4
	Meadows	528	2	1827	3529	0	0	0	7108	5655	18649	38.1	61.9
	Bare Soil	926	10	0	75	0	0	79	1792	2147	5029	42.7	57.3
	Total	7467	7653	3625	4749	518	949	928	8948	7939	42776		
	UA	47.6	16.1	49.6	0.0	0.2	99.7	87.8	79.4	27.0			
Co	Commission 5		83.9	50.4	100.0	99.8	0.3	12.2	20.6	73.0			
C	Overall Accu	41.15					Kappa:	0.309					

Table 1. Confusion matrix based on BF initialization method.

According to table 1, both Gravel and Asphalt classes have not been recognized. That's why Gravel class has spectral signatures nearly the same as Bricks class on the one hand, and on the other both Asphalt and bitumen have nearly the same spectral signatures. Figure 4 and 5 show these spectral similarities.



University Hyperspectral dataset.



Figure 5. Spectral signatures of similar classes in Pavia University Hyperspectral dataset.

In the second case, cluster centers are randomly initialized. Clustering results in this case have been shown in table 2.

		Classified											uo
		Gravel	Bitumen	Metal Sheets	Trees	Meadows	Bare Soil	Asphalt	Shadows	Bricks	Total	PA	Omissi
h	Gravel	0	357	0	0	2	2	42	0	1696	2099	0.0	100.0
	Bitumen	0	1166	0	0	0	0	1	0	163	1330	87.7	12.3
	Metal Sheets	0	3	1010	0	0	1	23	0	308	1345	75.1	24.9
LIZ	Trees	1144	0	5	1796	18	96	4	1	0	3064	58.6	41.4
Ground '	Meadows	3565	2	0	1833	7148	5670	9	0	422	18649	38.3	61.7
	Bare Soil	75	9	15	0	1813	2155	860	0	102	5029	42.9	57.1
	Asphalt	0	5743	3	0	13	24	64	2	782	6631	1.0	99.0
	Shadows	0	1	0	0	0	0	0	946	0	947	99.9	0.1
	Bricks	0	54	0	0	17	14	9	0	3588	3682	97.4	2.6
	Total	4784	7335	1033	3629	9011	7962	1012	949	7061	42776		
	UA	0.0	15.9	97.8	49.5	79.3	27.1	6.3	99.7	50.8			
Commission		100.0	84.1	2.2	50.5	20.7	72.9	93.7	0.3	49.2			
C	verall Accu	iracy:	41.78					Kappa:	0.315				

Table 2. Confusion matrix based on Random initialization method.

Like the first case, both Gravel and Asphalt classes have not been discriminated in this case. This is because of the above-mentioned reasons.

In the third case, initial position of cluster centers are obtained using MVES method. Clustering results of this case have been shown in table 3.

		Classified										on	
		Asphalt	Meadows	Bare Soil	Bitumen	Metal Sheets	Gravel	Shadows	Bricks	Trees	Total	PA	Omissi
	Asphalt	3489	19	56	2642	19	1	0	405	0	6631	52.6	47.4
	Meadows	368	14750	8	3	0	0	0	671	2849	18649	79.1	20.9
	Bare Soil	369	3388	822	17	3	0	0	425	5	5029	16.3	83.7
÷	Bitumen	20	0	1	1280	0	0	0	29	0	1330	96.2	3.8
nd Tru	Metal Sheets	0	0	1	6	816	510	0	12	0	1345	60.7	39.3
LOUI	Gravel	16	3	29	546	0	0	0	1505	0	2099	0.0	100.0
G	Shadows	1	0	0	0	0	0	946	0	0	947	99.9	0.1
	Bricks	12	14	2	234	0	0	0	3420	0	3682	92.9	7.1
	Trees	8	431	4	0	1	4	1	0	2615	3064	85.3	14.7
	Total	4283	18605	923	4728	839	515	947	6467	5469	42776		
	UA	81.5	79.3	89.1	27.1	97.3	0.0	99.9	52.9	47.8			
Co	mmission	20.7	10.9	72.9	2.7	100.0	0.1	47.1	52.2				
0	Overall Acc	uracy:	65.78					Kappa:	0.553				

Table 3. Confusion matrix based on MVES initialization method.

According to table 3, this case leads to highly better results than the other cases. As is obvious, using MVES method not only the best kappa coefficient are obtained but also Asphalt and Bitumen classes are discriminated. For comparative purpose, kappa coefficients and overall accuracies for three cases above are shown in figure 6.



Figure 6. Kappa coefficients and overall accuracies of kmeans clustering for different initialization methods.

As shown in figure 6, among these three methods, our proposed method with kappa coefficient of 55.3 leads into better result than BF and random methods with kappa coefficients of 3.09 and 31.5 respectively. Furthermore, unlike both BF and random method,

our proposed method is independent of iterations. In other words, our proposed method leads to the same result in different iterations.

5. CONCLUSION

In order to clustering of hyperspectral data, in this study, a multistep framework was presented to resolve the problem of initialization of k-means and improve the clustering efficiency. In the first step, HFC is used to estimate the number of endmembers in the image. Then, the spectral signatures of the endmembers are obtained using the MVES algorithm. Lastly, these spectral signatures are used to initialize the k-means clustering algorithm. The proposed method has been compared with two well-known initialization methods, namely, BF and Random methods. Clustering using MVES initialization method with kappa coefficient of 55.3 leads to highly better result than the other two methods. In other words, when MVES's spectral signatures are used as initial cluster centers, k-means clustering leads to the best result. More importantly, unlike the other two cases, using MVES's spectral signatures clustering leads to the same results in different iterations, which means, MVES method has the most stability. According to the confusion matrices in all three cases, despite the initial positions of cluster centers, the high spectral similarities of Asphalt and Bitumen classes on the one hand, and Gravel and Bricks classes, on the other, results in deteriorating clustering accuracy. To address last problem, either using another similarity measure or merging these two similar classes can be recommended.

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