

EVALUATING IMAGERY-DERIVED BATHYMETRY OF SEABED TOPOGRAPHY TO SUPPORT MARINE CADASTRE

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ABSTRACT:

The Department of Survey and Mapping Malaysia has introduced marine cadastre system to register the rights, other valid interests therein and ownership of spatially determined parcels in the context of the marine environment yet the implementation of the system is still at the rudimentary stage. One of the big issues here is gathering land-to-seabed data to create a seamless topographic base map to support its marine cadastre project. Seabed bathymetric mapping in coastal zone is one of the major components to support marine cadastre. In the past, accurate bathymetric measurements can be a very laborious task in hydrographic surveying. Traditional vessel-based acoustic soundings require a lot of time, operation cost and others. Today, human's ingenuity to yield bathymetric depths from multispectral images as an alternative source to chart the seabed topography has brought in new revolution to hydrography. The paper is initiated for evaluating water depth determination by using imagery-derived bathymetry technique and check its correlation with in-situ bathymetry depths. In the course of experiment, it demonstrates a good correlation between the imagery-derived bathymetric depths and the *in-situ* bathymetric depths, and majority of the derived depths have passed the minimum requirement of the IHO S-44 survey standard. The result also shows that these empirical models deliver promising outcome which can be use over the turbid environment setting. Hence, imagery-derived bathymetry approach can be an efficient and repeatable way to derive the seabed topography over a huge segment of coastal region. This study also suggests that imagery-derived bathymetry approach can be recognised as an aid in seabed topographic mapping to support marine cadastre initiative.

1. INTRODUCTION

In Malaysia, the hasty urbanization activities run not limited in coastal land, but also moving off the foreshore region. This massive land development has changed of patterns in property ownerships' management. Apparently, Department of Survey and Mapping Malaysia (DSMM) has introduced marine cadastre system to register the rights, other valid interests therein and ownership of spatially determined parcels in the context of the marine environment yet the implementation of the marine cadastre system is still at the rudimentary stage and many technical and legal issues need to be determined (Abdullah *et al.*, 2014; Nazirah & Abdullah, 2014). One of the big issues here is gathering land-to-seabed data to create a seamless topographic base map to support DSMM's marine cadastre project (Azhari *et al.*, 2017). The idea of having a Marine Geodetic Database (MGDB) for the development of a comprehensive Marine Spatial Data Infrastructure (MSDI) to facilitate security, marine cadastre, coastal geographical information system (GIS), economic development and environmental protection activities.

Apparently, more than sixty percent of the world's population today are living at the vulnerable coastal zone. Variations in the extremely versatile and dynamic coastal area can be associated to manmade activities as well as natural morphology alteration which happen either gradually or out of the sudden. Significant changes within a short period may not practical to be attempted using timely consuming ship-based sounding systems. Much of the coastal and shallow water zone remains unmapped, indeed poorly understood. In short, most of the navigation charts and topographic maps at those area is outdated and may not showing the possible hazards to the users.

Today, the ability of electromagnetic spectrum to penetrate water column has brought in new revolution the hydrographic surveying. The fundamental principle of extracting water depth information for bathymetric mapping using optical remote sensing data, a range of visible electromagnetic wavelengths (EMR) which can penetrate the water column in various degrees. This radiometric technique is first addressed by Lyzenga (1978) and further explored by Benny and Dawson (1983), Spitzer and Driks (1987), Jupp (1988), Philpot (1989), Bierwirth (1993), Maritorena *et al.* (1994), Dierssen *et al.* (2003), Stumpf *et al.* (2003) and updated by Lyzenga *et al.* (2006). These empirical, analytical and semi-analytical bathymetry retrieval methods are reportedly practical in clear coastal and shallow water for bathymetric mapping (Pacheco *et al.*, 2014; Jawak, Vadlamani, & Luis, 2015; Pe'eri *et al.*, 2013; Jégat *et al.*, 2016; Mavraeidopoulos *et al.* 2017).

For instance, the imagery-derived bathymetry technique has becoming popular and being employed as an alternative data acquisition technique over the shallow water and turbid tropical settings (Branmante *et al.*, 2013, Tang & Pradhan, 2015; Said *et al.*, 2017). The main reason is because this flexible technique does not require extensive amount of time, money and effort due to its vast spatial coverage (Gao, 2009; Jawak, Vadlamani, & Luis, 2015). This present study takes the initiative to evaluate the imagery-derived bathymetry's accuracy regarding the total vertical uncertainty (TVU) which are stipulated in International Hydrographic Organisation (IHO) Standards for Hydrographic Surveys Special Publication No.44 (S-44). Hence, the ultimate aim of this study is evaluating data quality of imagery-derived bathymetry mapping and its usability as an aid to support marine cadastre initiative.

2. DATA AND METHODOLOGY

This section outlines the characteristics of the study area and imagery-derived bathymetry approaches being adopted here to estimate the bathymetric depths from multispectral images. It briefly reviews on the selected imagery-derived bathymetry models, characteristics of the multispectral images, auxiliary data and image processing software as well as accuracy assessment being applied in this study.

2.1 Study Area

Malaysia is recognized as a maritime country with a total land mass of approximately 329,000 square kilometres, including 827 islands and 273 geographical entities within its 574,400 square kilometres marine jurisdiction. Its 4,809 kilometres

coastal belt varies from scenic bays flanked by rocky headlands to shallow mud flats lined with mangrove forests rich in biodiversity.

The authors conducted this study in southwest of Johor State, Malaysia, focused on a relatively small region. It made an attempt to determine the bathymetric depths of the study area, focusing at the shallow and near shore coastal waters as shown in Figure 1. It attempts to examine estimate the imagery-derived bathymetric depths lies between latitudes of $1^{\circ}18' N$ to $1^{\circ}21' N$ and longitudes of $103^{\circ}34' E$ to $103^{\circ}38' E$. Generally, the water bordering the study area is high turbidity which is also capable to represent majority of the west coast areas in Peninsular Malaysia. Typically, most of the swampy shoreface is fronted by flat slopes with highly turbid suspended sediments.

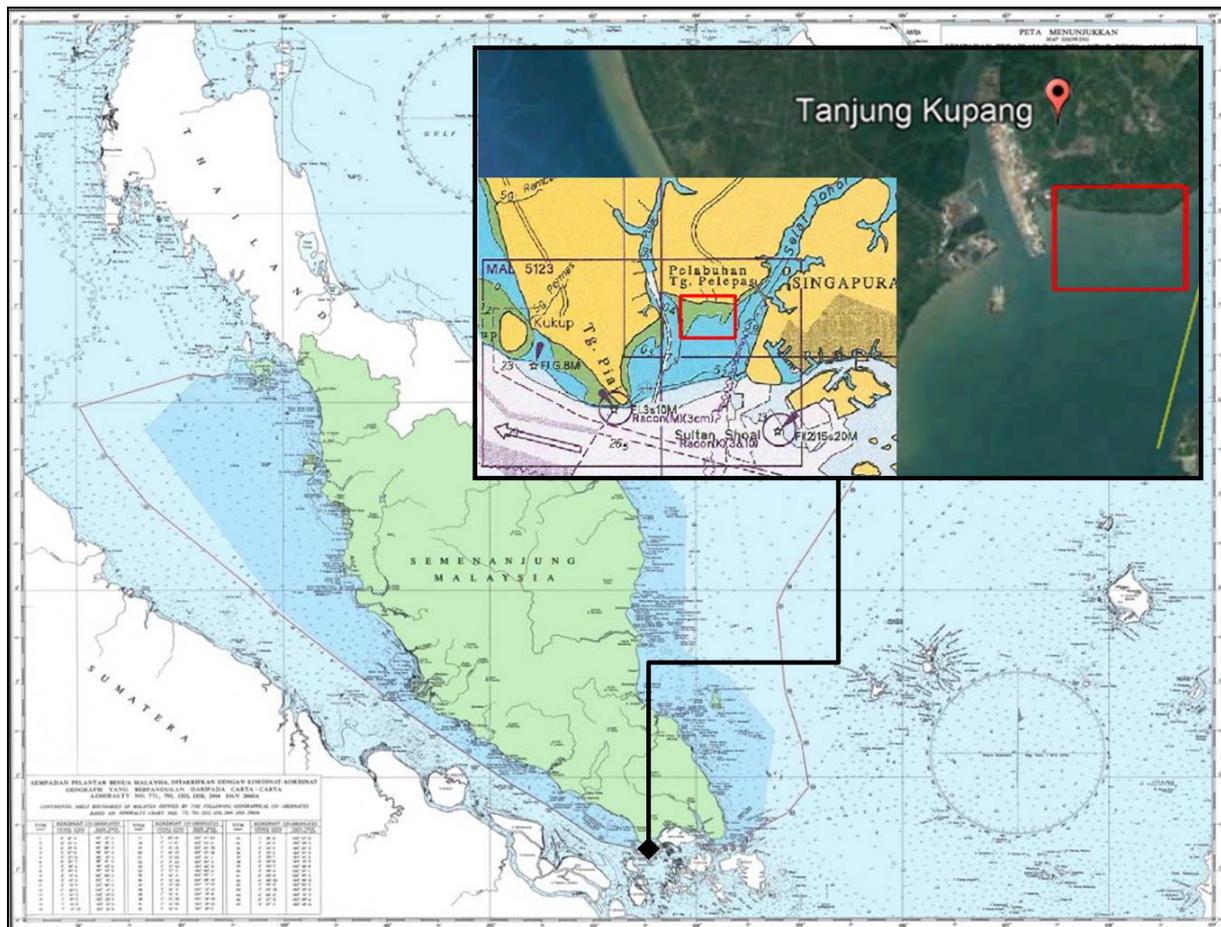


Figure 1. Coverage of the study area over the southwest of Johor state, Malaysia.

2.2 Methodology

This study incorporated the space-borne remote sensing and geographical information system (GIS) techniques to extract bathymetric depths from multispectral images. The overall research methodology and processing stages such as image pre-processing, image processing or bathymetric model construction as well as data verification to assess the data accuracy is shown in Figure 2.

Selection of imagery-derived bathymetry mapping was based on the condition of the satellite images, significantly spectral coverage, spectrum range and ground resolution. Prior

attempting to the image processing, pre-processing process like radiometric correction and atmospheric correction were applied to remove the atmospheric effects, unwanted path radiance as well as unnecessary sea surface reflectance, then followed by the geometric correction to correct the distortion of the images. Subsequent, tidally correlated SBES depths were separated into two different groups, briefly the training data and testing data. Training data was utilised to determine the most appropriate tuneable constant coefficient in the depth derivation algorithms. At the end of the process, the newly constructed linear regression models were evaluated using the known measurements from the group of testing data.

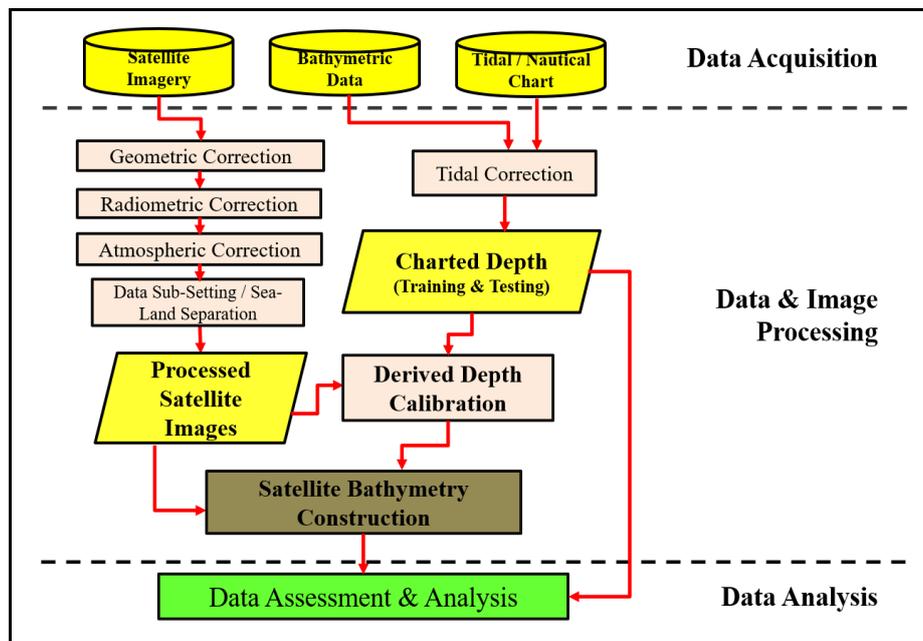


Figure 2. The overall methodology and processing stages performed in this study.

2.3 Multispectral Satellite Imagery

This dedicated study adopted freely downloadable Landsat-8 multispectral images acquired on 27th June 2013 for this feasibility study. For instance, only three spectral bands, blue spectrum (450-520nm), green spectrum (530-590nm) and NIR spectrum (850-880nm) were utilised to do this task. For instance, blue spectrum and green spectrum were used in the derivation algorithms. Thus, the near-IR (NIR) is proven to be effective in water and non-water areas separation (McFeeters, 1996; Canty, 2014). Conversely, green and NIR were utilised in the sea-land separation process, spatially filtered using Normalized Difference Water Index (NDWI).

These images were geo-referenced to the nautical chart by selecting an enough ground control points were widely scattered throughout the entire scene. Subsequently, the multispectral images were re-sampled into a relatively smaller area of which only cover the study area in order to optimize the image processing later. Image pre-processing process including radiometric correction, atmospheric correction and geometric correction were then being done order to eliminate the atmospheric effects, unwanted path radiance, unnecessary sea surface reflectance as well as the distortion of the images.

Advance and sophisticated remote sensing software such as ENVI 4.8 and ESRI ArcGIS 10.3 are proposed to be utilised in this study. Majority of the image pre-processing, processing and data generation were carried out using ENVI image processing software, while data manipulation and GIS analysis as well as map publishing were performed via ESRI ArcGIS software.

2.4 Bathymetric Depths Measurement

In-situ shipped-based single beam echo sounding survey (SBES) was commenced in August 2013. The accurate bathymetric depths throughout the entire study area were surveyed using a small hydrographic boat fitted with SBES synchronized with precise differential global positioning system (DGPS) positioning across the well-distributed survey lines with 5 metres interval and 25 metres line spacing.

Consequently, the tidally referenced *in-situ* bathymetric depths were divided into two groups. The first dataset was used to construct the depth-retrieval algorithm and another random dataset was set randomly for data assessment. A total of 1,367 check points was utilised for the final accuracy analysis at the end of the process.

2.5 Bathymetric Depth Derivation

This study attempted to yield the bathymetric depths over the shallow and turbid coastal region via two empirical approaches purposed by Dierssen *et al.* (2003) and Stumpf *et al.* (2003). Based on the fundamental principle of Beer-Lambert Law, both models implied the intensity of light decreases exponentially with depth, to relate the observed reflectance from the optical sensor to the water depth. Hence, the linear inversion approach can empirically derive the relationship between the pair of water-penetrating wavelengths.

2.5.1 Dierssen Model

Dierssen *et al.* (2003) has also developed a similar band-ratio concept to estimate the bathymetric depth (Z). It is presented slightly different by model the difference between observed reflectance log values. The estimated water depth is mathematically calculated from two tuneable constant coefficients (m_0 & m_1) and a log-difference between the observed reflectance of two consecutive bands (R_i & R_j). Equation 1 below demonstrates the Dierssen's log-ratio algorithm model:

$$Z = m_0 * \ln \left[\frac{nR_w(\lambda_i)}{nR_w(\lambda_j)} \right] + m_1 \quad (1)$$

Where,

- Z = depth value from derived depth
- R_w = observed reflectance of band i & j
- m_0 = tuneable constant for ratio to depth
- m_1 = offset of a depth
- n = constant value

2.5.2 Stumpf Model

Stumpf *et al.* (2003) has developed this simplified linear regression algorithm to determine the bathymetric depth (Z) from two tuneable constant coefficients (m_0 & m_1) and a ratio of observed reflectance of two consecutive bands (R_i & R_j). It uses the division between observed reflectance log values to estimate water depth. Equation 2 below illuminates the Stumpf's band ratio algorithm model:

$$Z = m_0 * \frac{\ln(R_w(\lambda_i))}{\ln(R_w(\lambda_j))} - m_1 \quad (2)$$

Where,

- Z = depth value from derived depth
- R_w = observed reflectance of band i & j
- m_0 = tuneable constant for ratio to depth
- m_1 = offset of a depth
- n = constant value

3. ACCURACY ASSESSMENT

Data assessment is an important step in the determining the usability of the manipulated data or commonly known as the quality assurance as well. Indeed, it involves a comparison of the water depth (z) which estimated from imagery-derived bathymetric modal against the vertical *in-situ* measurement value obtained from ship-based bathymetric survey. Accuracy assessment were tabled based on descriptive statistical analysis and IHO S-44 survey standards analysis.

3.1 Descriptive Statistical Analysis

Precision assessment was conducted using four difference statistical approaches such as mean error, standard error, standard deviation and variance. These computational procedures are basically simple numerical comparison base on the results obtained via imagery-derived bathymetric approach against the prior known value determined via field measurement work. This study utilised the outcomes of via imagery-derived bathymetric data from both models as a predicted value and the *in-situ* SBES data as the reference values.

3.2 IHO S-44 Survey Requirement

IHO S-44 is not a specification in neither hydrographic surveys nor nautical charting. Thus, it is only used as a standard by IHO member state for the compilation of its national nautical charts. Also, this publication does not contain procedures for setting up the necessary bathymetric survey equipment for data acquisition or for processing the resultant data. It only describes the minimum orders of survey stated in IHO S-44 that are considered acceptable to produce nautical charts across the surveyed area.

Table 1. IHO S-44's TVU minimum requirements for hydrographic surveys (modified from IHO, 2008).

Survey Order	TVU = $\sqrt{a^2 + (b \times d)^2}$			
	For this IHO Standards Assessment, value d = 10m			
	Special	1a	1b	2
Max allowable	a =	a =	a =	a =
TUV (95% Confidence level)	0.25m	0.25m	0.25m	0.25m
	b =	b =	b =	b =
	0.0075m	0.0075m	0.0075m	0.0075m
TVU	±0.261m	±0.517m	±0.517m	±1.026m

Due to the variation of seabed feature and water depth, four different orders of survey are defined to cater for a range of needs. In comparison, Table 1 shows the permissible TVU for Special Order is within 0.25 metre, Order 1a and 1b is below 0.5 metre and approximately 1.0 metre for Order 2 within 10 metres water depth).

4. RESULT AND ANALYSIS

This section presents the initial finding and results analysis of the imagery-derived bathymetry. Distinctly, Figure 3 to Figure 4 below illustrate the overall seabed topographical relief of the study area via digital elevation models and Table 2 and Table 3 show the statistical results and quantitative analysis of the IHO survey standard S-44 delivered by both Dierssen's and Stumpf's models.

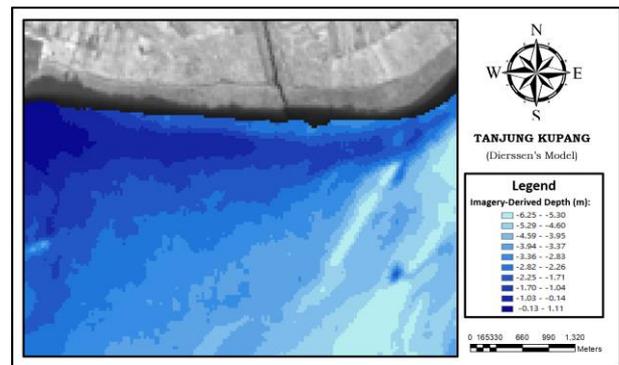


Figure 3. Imagery-derived bathymetric model from Dierssen's approach over the study area.

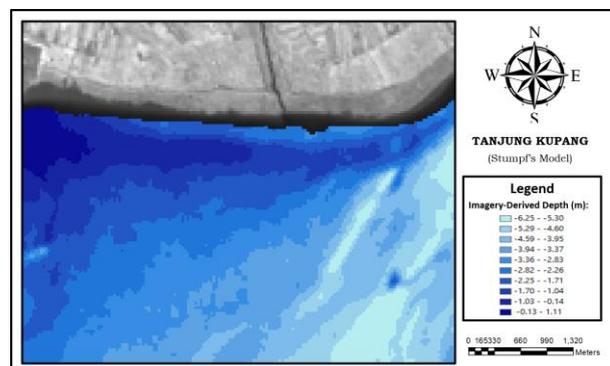


Figure 4. Imagery-derived bathymetric model from Stumpf's approach over the study area.

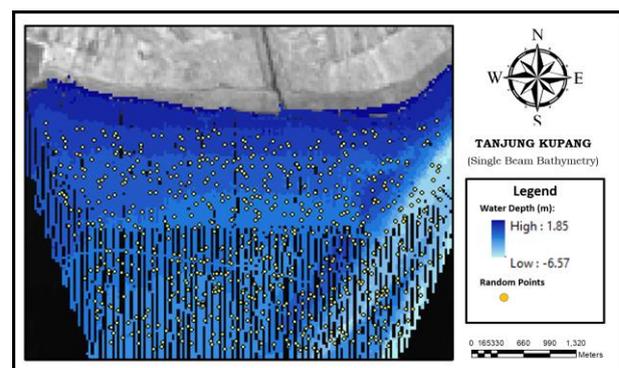


Figure 5: Location of the random points selected from the SBES data for depth validation.

In order to quantitatively evaluate and assess the accuracy of the imagery-derived bathymetry, data quality assessment was carried out using 1,367 check points, randomly picked out from the *in-situ* SBES dataset (Figure 5). The overall outcomes for both Dierssen’s and Stumpf’s derivation models are tabled in Table 2. In comparison, the result shows significant differences in mean error where Dierssen’s model produces 0.042 metres compared to 0.007 metres by Stumpf’s model. However, the standard error, standard deviation and variance for both derivation models are similar. The standard deviation for Dierssen’s is 0.674 metres, while Stumpf’s obtains 0.673 metres. Apart from that, both models also showing similar error range of 4.782 metres for Dierssen’s and 4.787 metres for Stumpf’s. Generally, the outcomes indicate that both imagery-derived bathymetry models provide satisfied results in this turbid water environment setting.

Table 2. Statistical results based on Dierssen’s and Stumpf’s models.

Statistical Analysis	Imagery-derived model	
	Dierssen Model	Stumpf Model
Mean error	0.042 m	0.007 m
Standard error	0.018 m	0.018 m
Standard deviation	0.674 m	0.673 m
Variance	0.455 m	0.454 m
Range	4.782 m	4.787 m
Minimum	-2.670 m	-2.639 m
Maximum	2.112 m	2.148 m

Subsequently, Table 3 illustrates the total vertical uncertainty (TVU) percentage achievement of IHO S-44 survey standard based on Stumpf’s model and Dierssen’s model achieved here. From a total of 1,367 depth samples, Stumpf’s model provides slightly higher passing rate than Dierssen’s model. Stumpf’s model produces a total of 1,215 (88.9%) depth samples that are able to meet the minimum IHO S-44 survey requirements. Whist, 1,211 (88.5%) depth samples out of the 1,367 depth samples from Dierssen’s model are able to pass the survey standards; while, there are 152 (11.1%) depth samples and 156 (11.4%) depth samples by Stumpf’s and Dierssen’s yet to comply the minimum requirement established in S-44, respectively.

Table 3. The passing rate of Dierssen’s and Stumpf’s models based on the IHO survey standard.

Details	Dierssen Model		Stumpf Model	
	Sample	Percentage	Sample	Percentage
Sample counts	1,367	100%	1,367	100%
IHO Passed	1,211	88.6%	1,215	88.9%
IHO Failed	156	11.4%	152	11.1%
Special order	513	37.5%	474	34.7%
Order 1a & 1b	370	27.1%	395	28.9%
Order 2	328	24.0%	346	25.3%

The table above also demonstrates the quantitative analysis in regards the survey order achieved by Dierssen’s and Stumpf’s models in their respective minimum requirements. Although the passing rate for Stumpf’s is higher, nonetheless the number of samples which successfully hit the Special Order class is only 474 (34.7%) depth samples. Undeniably, Dierssen’s delivers higher rate with 513 (37.5%) depth samples in Special Order class. Meanwhile, another 395 (28.9%) depth samples produce by Stumpf’s and 370 (27.1%) depth samples deliver from Dierssen’s are categorised in Order 1a and 1b classes, whereas 346 (25.3%) from Stumpf’s and 328 (24.0%) from Dierssen’s have achieved the minimum survey Order 2 standard as stated in IHO’s S-44.

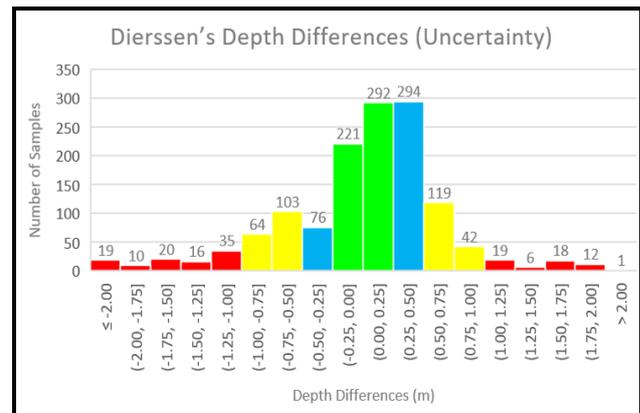


Figure 6. Distribution of depth differences and survey classes achievement from Dierssen’s model.

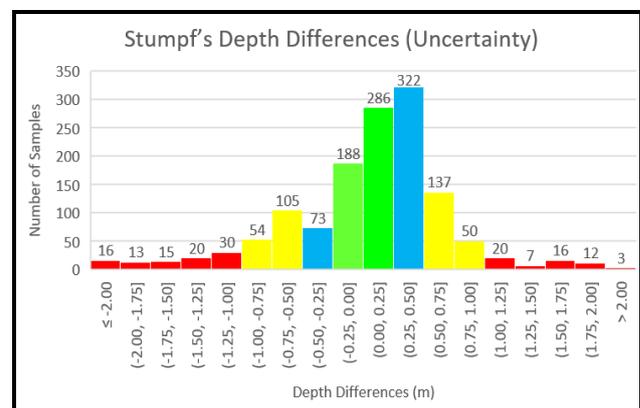


Figure 7. Distribution of depth differences and survey classes achievement from Stumpf’s model.

In contrast, histogram graph in Figure 6 and Figure 7 illustrate the distribution of depth differences from both Stumpf’s and Dierssen’s models in regard to various survey class. The x-axis is representing the error values, while the y-axis is showing the number of samples count. The outcomes are also arranged according to IHO S-44 survey order classes in histogram graphs, respectively. The green colour indicates the number of depth samples with the highest accuracy level (Special Order); the blue and yellow bars represent depth samples that achieving Order 1a & 1b and Order 2 survey standards respectively. In contrast, those bars plotted in red are the depth sample which failed to hit the minimum TVU set in IHO S-44.

5. CONCLUSION

In the completion of this study, the research goal and objectives are successfully attained. It examines the usability of satellite imagery-derived bathymetry in shallow and highly turbid waters in southwest of Johor state, Malaysia. A comparative analysis of two band ratio empirical models, namely the Dierssen's and Stumpf's models using the training data obtained from precise SBES survey. Principally, it has successfully demonstrated the level of accuracy in regard to the IHO S-44 survey requirements. Majority of the imagery-derived depths are relatively accurate, and it is capable and accomplished to meet the minimum total vertical uncertainty (TVU) survey specification.

Conversely, this study has enlightened that the imagery-derived bathymetry approach is possible to provide realistic seabed terrain profiles and three-dimensional quantitative information at the coastal and shallow water region. Although satellite-derived bathymetric mapping is an innovative solution to supplement the traditional vessel-based survey techniques, yet, it can be considered as an alternative tool in determining the seabed topography over broader coastal area in Malaysia to support the marine cadastre initiative.

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