

SNOW AVALANCHE SUSCEPTIBILITY MAPPING FOR DAVOS, SWITZERLAND

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ABSTRACT:

Snow avalanches are among destructive hazards occurring in mountainous regions and spatial distribution (susceptibility) of their occurrences needs to be considered for spatial planning and disaster risk mitigation efforts. The susceptibility assessment is the first step in avalanche disaster management and can be carried out using high resolution geospatial data and machine learning (ML) algorithms. In this study, we have assessed the snow avalanche susceptibility in Davos, Switzerland using an inventory delineated on satellite imagery in a previous study. The conditioning factors used for the avalanche susceptibility assessment include elevation, slope, plan curvature, profile curvature, aspect, topographic position index, topographic ruggedness index, topographic wetness index, land use and land cover, lithology, distance to road, and distance to the river. Two ML algorithms, the logistic regression (LR) and the random forest (RF), were comparatively assessed using validation data split from the training data (30/70). The prediction performances of both models were assessed based on the area under the receiver operating characteristic curve (ROC-AUC) value. Although the AUC value obtained from the LR method was relatively low (0.74), the value obtained from the RF (0.96) demonstrated high performance and usability of this approach. The results indicate that the RF method can successfully produce an avalanche susceptibility map for the region, although potential improvements may be possible by investigating various input features and ML algorithms as well as by classifying the starting and runout zones of the avalanche data separately. Furthermore, the accuracy is expected to increase by using a larger training dataset.

1. INTRODUCTION

Snow avalanches are among widely observed natural hazards affecting human life, economy, infrastructure, vegetation, and geomorphology in mountainous and cold regions. A snow avalanche is defined as a rapidly moving mass of snow on steep slopes (Schweizer et al., 2003). Snow avalanche susceptibility is the spatial probability for avalanche occurrence. Avalanche susceptibility assessment is the first and essential stage of the hazard and risk assessment for disaster management and mitigation.

Scientific analysis of snow avalanches has become crucial to mitigate risks through modeling, mapping, visualizing, and monitoring of susceptible regions with the help of Geographic Information Systems (GIS) and remote sensing (RS) (Yilmaz, 2010; Kumar et al., 2016). Field-based studies are limited by the high-risk exposure and can be time-consuming due to the snow mass instability and adverse weather conditions, compared to the GIS and remote sensing-based approaches (Eckerstorfer et al., 2016). On the other hand, GIS and RS are significant and cost-effective tools for avalanche assessments (Bühler et al., 2018).

The occurrence of avalanche hazards depends on the conditioning and the triggering factors (Nefeslioglu et al., 2013). The snowpack characteristics (e.g., thickness, stability, density, water content, grain size, etc.), the atmospheric conditions (e.g., air temperature, precipitation, wind speed, wind direction, etc.), and topographical factors (elevation, slope, curvature, aspect, ground cover, etc.) have frequently been considered as conditioning factors for avalanches in the literature. Rapid

temperature changes, heavy rainfalls, earthquakes, and anthropogenic activities are the triggering factors that initiate the snow mass movement (Hao et al., 2018; Kumar et al., 2017; Nefeslioglu et al., 2013).

Researchers have applied various expert-based techniques for avalanche susceptibility mapping (ASM) such as fuzzy-frequency ratio (FR) (Kumar et al., 2016), analytical hierarchical process (AHP) (Nefeslioglu et al., 2013; Selçuk, 2013), etc. The data-driven machine learning (ML) applications have made great strides for natural hazard assessments in recent years due to the ability to learn, predict and improve based on historical hazard events without human intervention; and the capability of trend and pattern identification as well as dealing with multi-dimensional and multi-source data such as conditioning and triggering factors. Although various ML applications exist on floods and landslides, the mechanism for ASM has not been clearly understood due to the difficulties in inventory preparation.

Mosavi et al. (2020) implemented an ensemble ML model, random subspace functional tree (RSFT), and compared the model outcome with the other ML methods such as logistic regression (LR), logistic model tree (LMT), alternating decision tree (ADT), and functional trees (FT) for Karaj Watershed, Iran. Tiwari et al. (2021) applied a Support Vector Machine (SVM) to predict avalanche susceptibility with 4 different kernel approaches. Akay (2021) indicated that the Random Forest (RF) is appropriate for ASM. Rahmati et al. (2019a) comparatively evaluated various ML methods for avalanche susceptibility map (ASM) production at two different sites and found the RF method

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very successful. Choubin et al. (2020) employed a generalized additive model (GAM), multivariate adaptive regression spline (MARS), boosted regression trees (BRT), and SVM for comparing ensemble ML methods. The results from the mentioned studies have shown that the ML methods can provide a useful estimate for avalanche susceptibility.

In this study, the LR and the RF, which are commonly used ML methods, were implemented to produce the ASM of Davos (Switzerland) using a total of twelve conditioning factors, such as elevation, slope, plan curvature, profile curvature, aspect, topographic position index (TPI), topographic ruggedness index (TRI), topographic wetness index (TWI), land use/ land cover, lithology, distance to road, distance to the river. The avalanche inventory was prepared in a previous study by Hafner et al. (2021a) in the form of vector data (polygons) and provided for the purposes of the present study to be employed as the training data for the supervised ML methods mentioned above. The other input features (conditioning factors) were derived from the geospatial datasets obtained from Swiss Federal Office of Topography, Switzerland (Swisstopo). In the following Sections, the datasets, methods, and the ASM results are presented in detail and discussed accordingly.

2. MATERIALS AND METHODS

In this Section, the study area characteristics, the input datasets and the pre-processing methods as well as the ML methods and the validation approaches are explained in detail. The location of the study area is shown in Figure 1. The overall methodological workflow employed in the study is presented in Figure 2.

2.1 Study Area

The study area, Davos, is located in the Eastern Region of Switzerland. Snow avalanche hazards occur frequently in the region due to climatic and topographic characteristics. The study area covers approximately 336 km² and has an altitude range from 1,158 m to 3,144 m. According to the Institute for Snow and Avalanche Research (SLF), Switzerland, 17 people lost their lives in Davos region due to snow avalanches during 2002 - 2021 (SLF, 2021). The geology of the region is characterized by Lower Penninic- Upper Austroalpine plate boundary (Ferreiro Mählmann and Giger, 2012). The study area comprises southeast of the Prättigau halfwindow and lies below the Silvretta nappe (Nagel, 2006). The western part of the study area covers mostly Upper Austroalpine sediments and volcanites. In the eastern part, crystalline formations of the Silvretta nappe consist mainly of metamorphic rocks (gneiss, mica slate, amphibolite).

2.2 Input Datasets and Features

A reliable and complete inventory is essential to determine the effects and the characteristics of avalanches (Tiwari et al., 2021). The avalanche inventory was manually produced by Hafner et al. (2021b) for two avalanche periods in 2018 and 2019 from satellite images and provided for the present study. The inventory (Hafner et al., 2021b) includes the location information in the form of polygons. Figure 1 shows the avalanche inventory and 3D views of some parts. Two avalanche polygons with runout zones in the valley were not employed in the model training stage since they may increase the uncertainty in the models. The avalanche inventory map was rasterized prior to model training and the avalanche and non-avalanche pixels were labeled as True (1) and False (0), respectively.

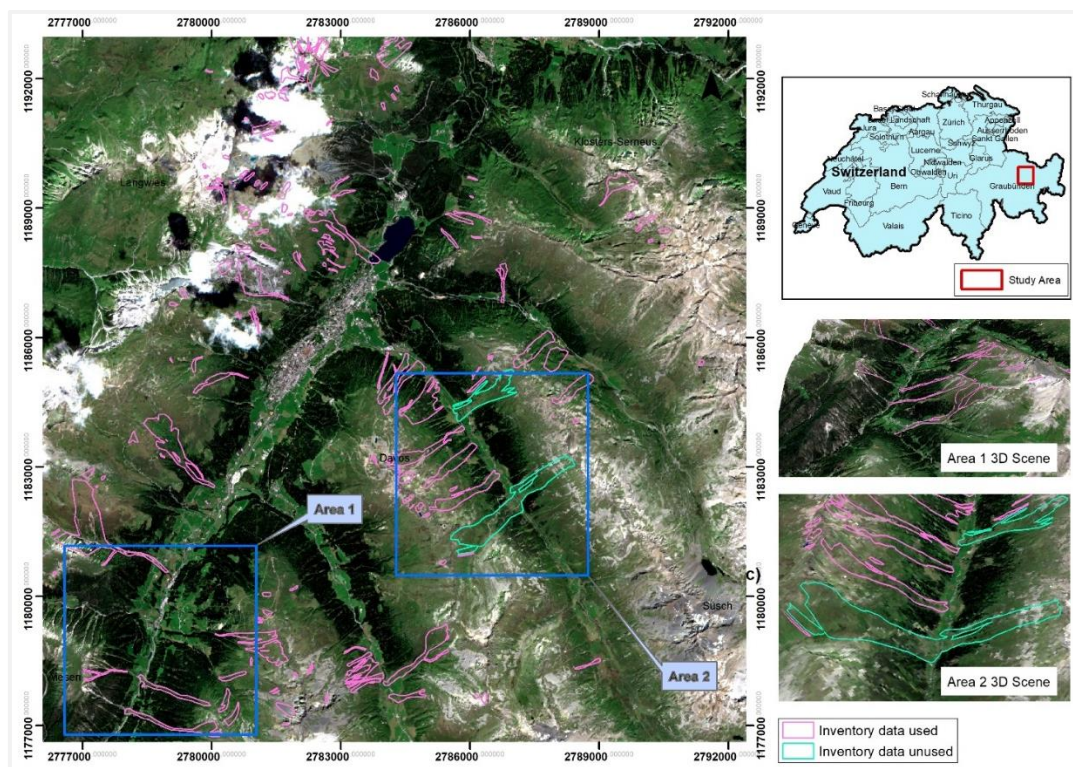


Figure 1. The location map, the satellite image of the study site and the avalanche inventory.

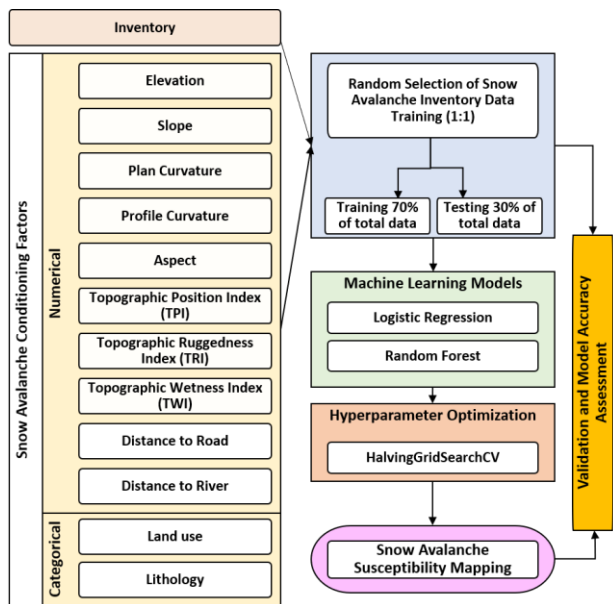


Figure 2. Flowchart of the methodology.

The slope is an important component of avalanche susceptibility studies, owing to avalanches generally occurring on snow-covered slopes between 30°-45° (Schweizer and Jamieson, 2003). Aspect can be defined as the direction of a terrain associated with a compass. Although snow avalanches tend to occur from all aspects, the reported literature cases have shown that northern regions are more prone to avalanches (Winkler et al., 2021). The term curvature is used for describing the morphology of slope, which is an important factor for snow cover stability (Akay, 2021). The plan and profile curvatures affect snow-mass movement into horizontal and vertical directions, respectively. The TPI refers to the change in elevation of a central point and mean height of a predefined set of neighboring points (Wilson and Gallant, 2000). A study conducted by Choubin et al. (2020) has shown that the TPI was among the most significant factors for four different avalanche susceptibility prediction models. The TRI is a parameter that measures the surface roughness, which may affect snowpack destabilization (Kumar et al., 2017). The TWI provides information about the hydrological condition of topography (Rahmati et al., 2019b).

The digital elevation model (DEM) employed in the study (swissALTI3D) was freely provided by Swisstopo (2021), and was downsampled here to 10 m spatial resolution for computational reasons. The slope, plan curvature, profile curvature, aspect, TPI, TRI, and TWI were calculated from the 10 m DEM using the SAGA GIS software (Conrad et al., 2015). According to Parshad et al. (2017), it may be difficult to indicate the direct effect of elevation on snow avalanche hazards. Yet, it must be taken into account for the terrain perspective to be exposed to precipitation, temperature, and wind. In addition, distance to river and distance to road factors were calculated with proximity grid module in SAGA GIS and stored in raster format.

The lithological units in a region can affect heat absorption and transfer, which may lead to snow mass movement and avalanches (Choubin et al., 2020). Considering the land use and land cover (LULC) and the avalanche relationship, several researchers emphasized that avalanches frequently occur on grassland and bare land (Bergua et al., 2018; Maggioni et al., 2016; Suk and Klimánek, 2011). Even though some avalanches were observed in forests, it was concluded in some studies that the forests were also effective in reducing the avalanche risk (Varol, 2022).

In this study, the conditioning factors were used as model input and divided into two categories as numerical and categorical. The lithology and LULC data were considered as categorical features. Table 1 provides the distribution of lithological and LULC cover units by pixel for avalanche and non-avalanche areas. According to the inventory data, the avalanches occurred mostly in gneiss and mica slate, metagranitoids, sedimentary rocks as lithological units. Remarkably, 65.94% of avalanches occurred on grassland, 21.99% rock (bare land), 11.40% forest, considering LULC.

Lithological Units	Non - Avalanche	Avalanche
Alluvium	40,455	128
Amphibolite	243,105	7927
Basalt and metabasalt	24,450	-
Gneiss and mica slate	904,259	27,828
Glacier	9692	-
Mainly blocks (rockslide)	249,511	4955
Meta-ultrabasite, metabasalt, metagabbro	24,093	2956
Metagranitoids	495,286	20,003
Moraine	452,969	9870
Rhyolite, dacite	69,889	2904
Sedimentary rocks	541,582	18,785
Serpentinite, talc schist	91,361	2336
Tectonic melange	36,628	2407
Water	6818	350
Land use / Land cover Units		
Forest	616,099	11,450
Glacier	1408	-
Grassland	1,594,527	66,238
Rock	922,902	22,091
Settlement	33,030	28
Water	22,132	642

Table 1. The pixel counts of categorical factors.

Figure 3 shows the conditioning factors as maps (1821 x 1807 pixels each at 10 m size). The pixels employed as non-avalanche class in the training dataset were randomly selected with an equal number to avalanche class pixels (a ratio of 1:1 for avalanche: non-avalanche). In the second step, the dataset was randomly split as training (70%) and validation (30%) datasets for avalanche prediction based on LR and RF. Open source scikit-learn library Pedregosa et al. (2011) was used for processing the methods in a Python environment.

Table 2 demonstrates the statistical summary of avalanche and non-avalanche areas for the numerical features. The statistical metrics include the mean, standard deviation, minimum, 25%, 50%, 75%, maximum.

2.3 Snow Avalanche Susceptibility Mapping

In this study, the LR and the RF methods were evaluated for their prediction performances. The LR is an important and frequently used statistical tool for binary classification problems (Mosavi et al., 2020). The method measures the relationship of variables with logistic curves, similar to linear regression (Yariyan et al., 2020). In this study, LR was used to estimate the avalanche and non-avalanche probability of the study area. The `sklearn.linear_model.LogisticRegression` library was applied with `"C = 100, solver = 'lbfgs', class_weight = 'balanced'"` parameters as a result of hyperparameter tuning.

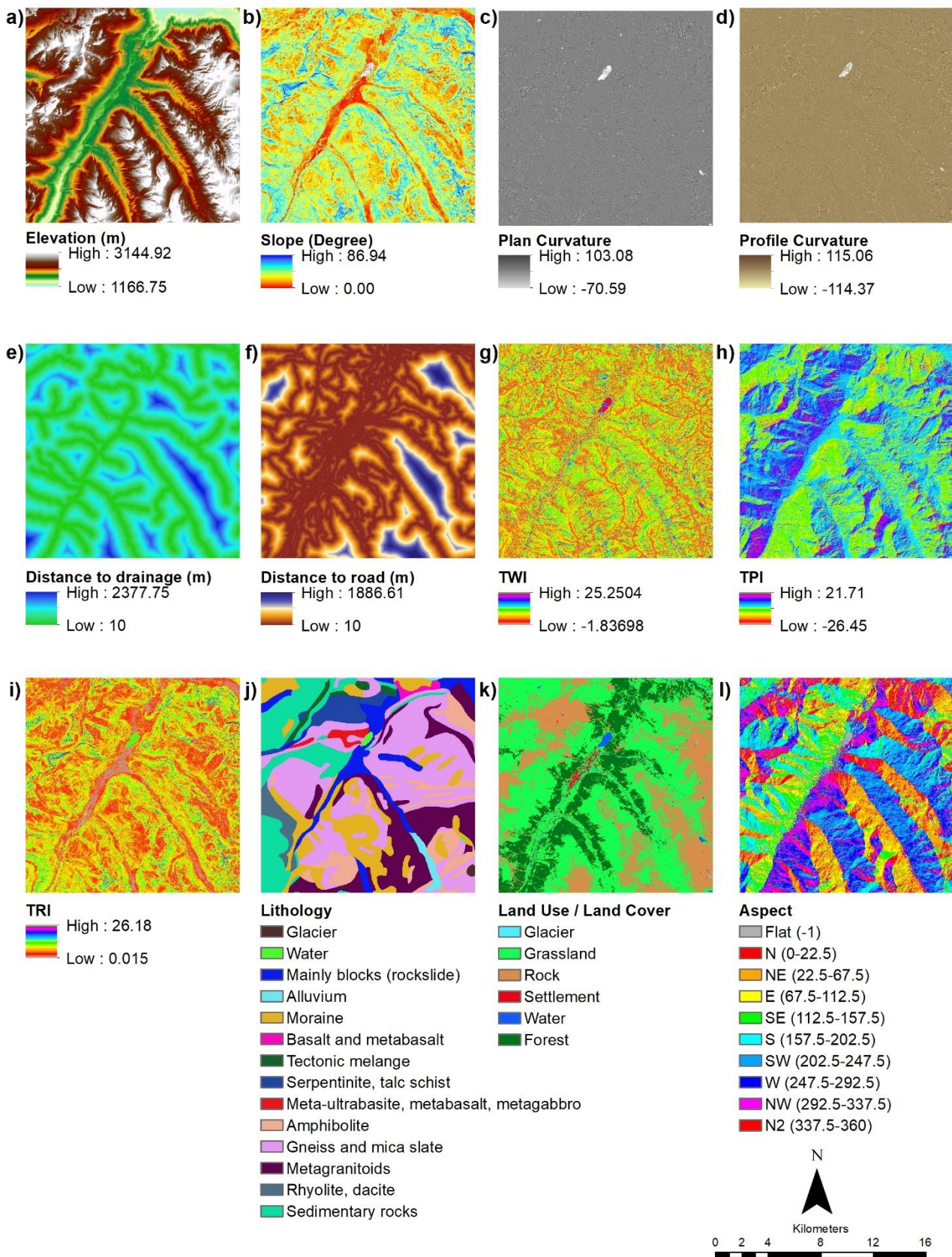


Figure 3. Input features: (a) elevation, (b) slope, (c) plan curvature, (d) profile curvature, (e) distance to the drainage, (f) distance to road, (g) topographic wetness index (TWI), (h) topographic position index (TPI), (i) topographic ruggedness index (TRI), (j) lithology, (k) land use/ land cover, (l) aspect.

Factors		Mean	Std. Dev	Min	25%	50%	75%	Max
Elevation	Non-avalanche	2121.17	369.71	1166.75	1852.67	2150.17	2401.67	3144.92
	Avalanche	2129.80	264.81	1369.87	1944.35	2145.33	2338.95	2811.40
Slope	Non-avalanche	26.71	12.48	0.00	17.57	26.98	35.19	86.94
	Avalanche	29.96	10.74	0.00	23.03	30.83	37.14	81.77
Aspect	Non-avalanche	178.92	104.36	-1.00	81.25	188.85	266.22	360.00
	Avalanche	141.78	94.56	-1.00	55.62	128.85	214.44	360.00
Profile Curvature	Non-avalanche	0.02	2.16	-114.38	-0.72	0.06	0.84	115.06
	Avalanche	0.19	1.89	-29.05	-0.57	0.15	0.92	33.57
Plan Curvature	Non-avalanche	0.03	2.30	-70.59	-0.88	0.02	0.92	103.08
	Avalanche	-0.21	2.36	-25.13	-1.12	-0.09	0.83	26.45
TRI	Non-avalanche	0.84	0.52	0.00	0.49	0.79	1.09	26.19
	Avalanche	0.94	0.43	0.00	0.66	0.92	1.17	10.94
TPI	Non-avalanche	-0.04	0.62	-26.45	-0.40	-0.03	0.32	21.72
	Avalanche	0.12	0.56	-5.22	-0.21	0.13	0.48	5.07
TWI	Non-avalanche	5.32	2.08	-1.84	3.90	5.05	6.38	25.25
	Avalanche	5.67	2.10	0.19	4.29	5.43	6.71	23.83
Distance to Drainage	Non-avalanche	532.16	375.94	0.00	228.04	472.02	770.06	2377.75
	Avalanche	526.74	339.15	0.00	224.72	512.45	800.50	1667.09
Distance to Roads	Non-avalanche	309.25	335.72	0.00	60.00	183.85	444.07	1886.61
	Avalanche	230.67	211.56	0.00	63.25	170.00	345.40	1381.92

Table 2. Summary statistics of the numerical features.

The RF is a tree-based ensemble learning algorithm, that was first proposed by Breiman (2001) and is widely used for classification and regression problems. The method creates trees from randomly selected data with the bootstrap technique. The sklearn.ensemble.RandomForestClassifier library was implemented with “*n_estimators = 250, criterion = 'entropy', max_depth = 16, max_features = 16, class_weight = 'balanced_subsample', oob_score = 'true', bootstrap = 'true'*” parameters. The parameters with the highest accuracy were selected, as a consequence of the hyperparameter optimization.

In order to improve the model performances, the HalvingGridSearchCV method was utilized for the hyperparameter optimization (HalvingGridSearchCV, 2022). The optimal values obtained from the method were applied in the prediction. In the third step, overall accuracy (OA), the receiver operating characteristics (ROC) curve and area under the curve (AUC) value were produced to evaluate the performances.

3. RESULTS

The OA of the LR model was found 0.66. The result of the prediction was verified using the ROC (Figure 4) and an AUC value of 0.74 was obtained. Figure 5 illustrates the color gradient distribution of the probabilities acquired from the LR model. The OA of the RF model was found 0.88. Figure 6 indicates the performance of the predictive model using the ROC and an AUC value of 0.96 was obtained from the RF. Figure 7 shows the gradient map of the probabilities obtained from the RF model.

The ASMs were classified as very low (0 - 0.2), low (0.2 - 0.4), moderate (0.4 - 0.6), high (0.6 - 0.8) and very high (0.8 - 1.0) susceptibilities by using equal intervals. In ASM obtained from the LR shows that 17.95% of the study area has very low, 30.82% low, 29.43% moderate, 18.62% high, 3.17% very high susceptibility classes. As a result of the RF, 64.24% of the study area has very low, 15.49% low, 10.62% moderate, 7.31% high, 2.34% very high susceptibility classes. In Figure 8 shows the probability distribution histograms obtained from both methods. While the LR provides a normal distribution, the RF results yield

to a geometric distribution of the outputs. Based on the maps and the statistical summaries mentioned previously, it can be concluded that the LR method possibly overestimates the areas susceptible to avalanches. This situation also explains the lower OA value obtained from this model.

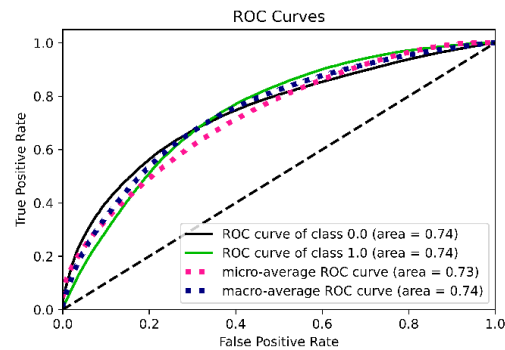


Figure 4. The ROC curve obtained from the LR

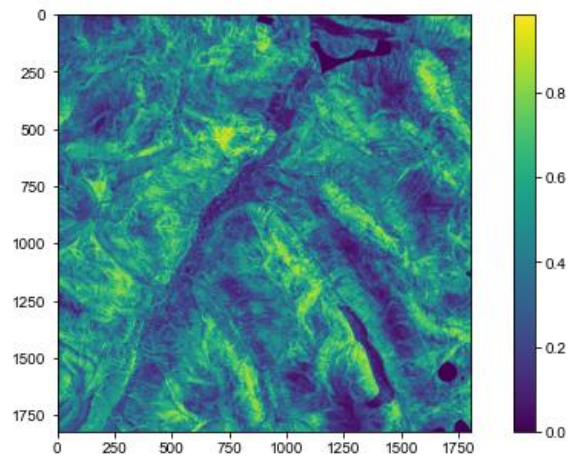


Figure 5. The spatial distributions of the avalanche probabilities obtained from the LR.

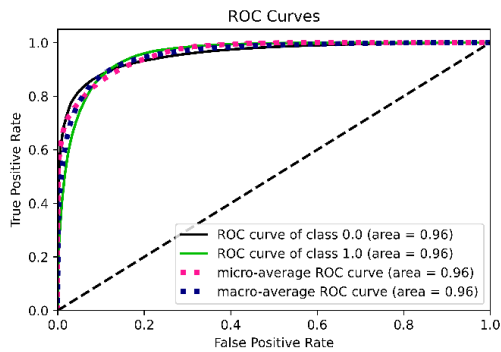


Figure 6. The ROC curve obtained from the RF.

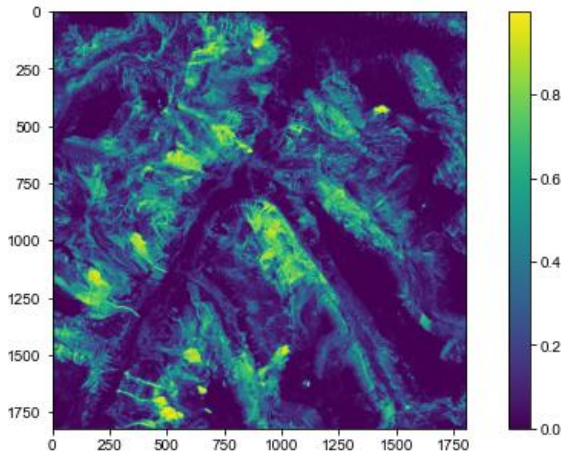


Figure 7. The spatial distributions of the avalanche probabilities were obtained from the RF.

On the other hand, when the sub-areas given in Figure 9 are analyzed in detail; it can be emphasized that the RF determined the avalanche zones with higher susceptibility levels. However, when the two avalanche polygons, which were not used in model training due to the inclusion of runout zones, are analyzed; the LR exhibited higher susceptibility levels for those. This finding indicates that the selection of training zones and the feature importance obtained from both methods must be investigated to understand the results and to obtain higher accuracy.

4. DISCUSSIONS AND CONCLUSIONS

A snow avalanche is a frequently observed natural hazard threatening lives and properties in mountainous and cold regions. The ASMs can be used as a basemap or initial data by researchers, designers, and decision-makers for regional land use planning, site selection, and avalanche prevention and mitigation purposes. In the present study, the LR and RF models were employed for snow ASM with 12 conditioning factors in Davos, Switzerland. The training data (Hafner et al., 2021b) was produced in a previous study for two avalanche periods and provided by the SLF.

The results show that the AUC value of the RF (0.96) was better than the LR (0.74), which indicates that the RF exhibited higher prediction performance for the study area. However, further attention needs to be paid to the training data selection to prevent from model overfitting, and the input features to utilize the most suitable ones in the modeling stage. In addition, testing and validation datasets must be selected properly for increasing the accuracy and the reliability of the models. Furthermore, the avalanche inventory dataset (Hafner et al., 2021b) was limited to two avalanche periods only, and a larger inventory can contribute towards a better understanding of avalanche susceptibility analysis and to obtain higher accuracy.

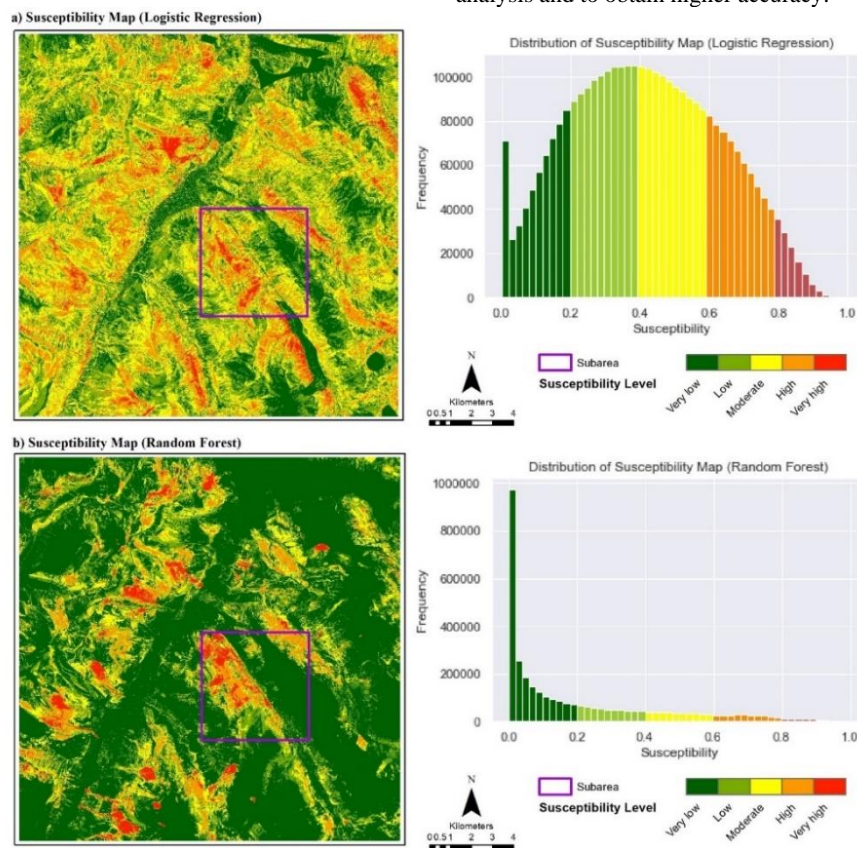


Figure 8. Avalanche susceptibility maps and distributions of LR (a) and RF model (b).

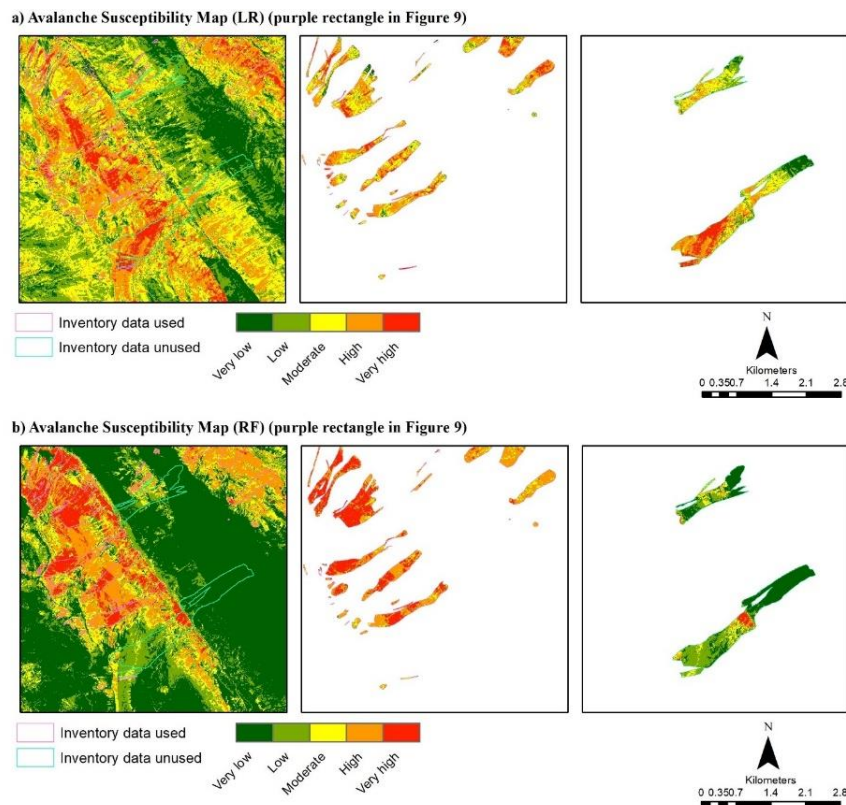


Figure 9. The LR (a) and RF (b) results in a part of the study area (purple rectangle in Figure 9). The two avalanche polygons shown on the right column were not employed in model training.

The recent ASM studies based on ML algorithms have shown promising results. Wen et al., (2022) employed SVM, K-nearest neighbors, Classification and Regression Tree, and Multilayer perceptron and to compare the prediction capability with the AUC values of 0.918, 0.906, 0.879, 0.909, respectively. Rahmati et al. (2019b) applied BRT, GAM, SVM methods for prediction of avalanche susceptibility in an area in Iranian watershed. The AUC value obtained from the SVM was 0.924, indicating high performance of this model. Akay (2021) investigated several ML methods such as evidential belief function (EBF), random tree (RT), RF, and AdaBoost M1, etc.; and obtained AUC values of 0.990 for training and 0.978 for testing from EBF. Rahmati et al. (2019a) conducted a comparative study with RF, SVM, Naïve Bayes and GAM models for the Darvan and the Zarrinehroud watersheds and found the RF successful in both Darvan (AUC = 0.964) and Zarrinehroud (AUC = 0.956). When the results presented in this study are compared with those mentioned above, it can be emphasized that the performance of the RF was also very high here and it is a suitable method for ASM production.

As future work, the model inputs will be analyzed in terms of feature importance and further ML methods will be assessed. Snowpack knowledge, additional terrain features and meteorological conditions could be useful to developing the ASMs. Furthermore, the inventory data used here will be analyzed to separate the starting and runout zones.

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REFERENCES

- Akay, H., 2021. Spatial modeling of snow avalanche susceptibility using hybrid and ensemble machine learning techniques. *Catena* 206, 105524. <https://doi.org/10.1016/j.catena.2021.105524>
- Bergua, S.B., Piedrabuena, M.Á.P., Alfonso, J.L.M., 2018. Snow avalanche susceptibility in the eastern hillside of the aramo range (Asturian central massif, cantabrian mountains, nw Spain). *J. Maps* 14, 373–381. <https://doi.org/10.1080/17445647.2018.1480974>
- Breiman, L., 2001. Random forests. *Mach. Learn.* 45, 5–32. <https://doi.org/10.1023/A:1010933404324>
- Bühler, Y., Von Rickenbach, D., Stoffel, A., Margreth, S., Stoffel, L., Christen, M., 2018. Automated snow avalanche release area delineation-validation of existing algorithms and proposition of a new object-based approach for large-scale hazard indication mapping. *Nat. Hazards Earth Syst. Sci.* 18, 3235–3251. <https://doi.org/10.5194/nhess-18-3235-2018>
- Yilmaz, B., 2010. Application of GIS-Based Fuzzy Logic and Analytical Hierarchy Process (AHP) to Snow Avalanche Susceptibility Mapping, North San Juan, Colorado. Karadeniz Technical University.
- Choubin, B., Borji, M., Hosseini, F.S., Mosavi, A., Dineva, A.A., 2020. Mass wasting susceptibility assessment of snow avalanches using machine learning models. *Sci. Rep.* 10, 1–13. <https://doi.org/10.1038/s41598-020-75476-w>
- Conrad, O., Bechtel, B., Bock, M., Dietrich, H., Fischer, E., Gerlitz, L., Wehberg, J., Wichmann, V., Böhner, J., 2015. System for Automated Geoscientific Analyses (SAGA) v. 2.1.4. *Geosci. Model Dev.* 8, 1991–2007. <https://doi.org/10.5194/gmd-8-1991-2007>

2015 (4 November 2021)

Eckerstorfer, M., Bühler, Y., Frauenfelder, R., Malnes, E., 2016. Remote sensing of snow avalanches: Recent advances, potential, and limitations. *Cold Reg. Sci. Technol.* 121, 126–140. <https://doi.org/10.1016/j.coldregions.2015.11.001>

Ferreiro Mählmann, R., Giger, M., 2012. The Arosa zone in Eastern Switzerland: Oceanic, sedimentary burial, accretional and orogenic very low- to low grade patterns in a tectono-metamorphic mélange. *Swiss J. Geosci.* 105, 203–233. <https://doi.org/10.1007/s00015-012-0103-7>

Hafner, E.D., Techel, F., Leinss, S., Bühler, Y., 2021a. Mapping avalanches with satellites – evaluation of performance and completeness. *Cryosph.* 15, 983–1004. <https://doi.org/10.5194/tc-15-983-2021>

Hafner, E., Leinss, S., Techel, F., Bühler, Y., 2021b. Satellite avalanche mapping validation data. <https://doi.org/http://dx.doi.org/10.16904/envidat.2021> (20 December 2021)

HalvingGridSearchCV, 2022. URL https://scikit-learn.org/stable/modules/generated/sklearn.model_selection.HalvingGridSearchCV.html

Hao, J. sheng, Huang, F. rong, Liu, Y., Amobichukwu, C.A., Li, L. hai, 2018. Avalanche activity and characteristics of its triggering factors in the western Tianshan Mountains, China. *J. Mt. Sci.* 15, 1397–1411. <https://doi.org/10.1007/s11629-018-4941-2>

Kumar, S., Snehmani, Srivastava, P.K., Gore, A., Singh, M.K., 2016. Fuzzy–frequency ratio model for avalanche susceptibility mapping. *Int. J. Digit. Earth* 9, 1168–1184. <https://doi.org/10.1080/17538947.2016.1197328>

Kumar, S., Srivastava, P.K., Snehmani, 2017. GIS-based MCDA–AHP modelling for avalanche susceptibility mapping of Nubra valley region, Indian Himalaya. *Geocarto Int.* 32, 1254–1267. <https://doi.org/10.1080/10106049.2016.1206626>

Maggioni, M., Godone, D., Höller, P., Oppi, L., Stanchi, S., Frigo, B., Freppaz, M., 2016. Snow gliding susceptibility: the Monterosa Ski resort, NW Italian Alps. *J. Maps* 12, 115–121. <https://doi.org/10.1080/17445647.2016.1167785>

Mosavi, A., Shirzadi, A., Choubin, B., Taromideh, F., Hosseini, F.S., Borji, M., Shahabi, H., Salvati, A., Dineva, A.A., 2020. Towards an Ensemble Machine Learning Model of Random Subspace Based Functional Tree Classifier for Snow Avalanche Susceptibility Mapping. *IEEE Access* 8, 145968–145983. <https://doi.org/10.1109/ACCESS.2020.3014816>

Ferreiro Mählmann, R., Giger, M., 2012. The Arosa zone in Eastern Switzerland: Oceanic, sedimentary burial, accretional and orogenic very low- to low grade patterns in a tectono-metamorphic mélange. *Swiss J. Geosci.* 105, 203–233. <https://doi.org/10.1007/s00015-012-0103-7>

Nefeslioglu, H.A., Sezer, E.A., Gokceoglu, C., Ayas, Z., 2013. A modified analytical hierarchy process (M-AHP) approach for decision support systems in natural hazard assessments. *Comput. Geosci.* 59, 1–8. <https://doi.org/10.1016/j.cageo.2013.05.010>

Parshad, R., Srivastva, P.K., Snehmani, Ganguly, S., Snehmani, Snehmani, 2017. Snow Avalanche Susceptibility Mapping using Remote Sensing and GIS in Nubra-Shyok Basin, Himalaya, India. *Indian J. Sci. Technol.* 10, 1–12. <https://doi.org/10.17485/ijst/2017/v10i31/105647>

Pedregosa, F., Grisel, O., Weiss, R., Passos, A., Brucher, M., Varoquax, G., Gramfort, A., Michel, V., Thirion, B., Grisel, O., Blondel, M., Prettenhofer, P., Weiss, R., Dubourg, V., Brucher, M., 2011. Scikit-learn: Machine Learning in Python. *J. Mach. Learn. Res.* 12, 2825–2830. (20 December 2021)

Rahmati, O., Ghorbanzadeh, O., Teimurian, T., Mohammadi, F., Tiefenbacher, J.P., Falah, F., Pirasteh, S., Ngo, P.T.T., Bui, D.T., 2019a. Spatial modeling of snow avalanche using machine learning models and geo-environmental factors: Comparison of effectiveness in two mountain regions. *Remote Sens.* 11. <https://doi.org/10.3390/rs11242995>

Rahmati, O., Yousefi, S., Kalantari, Z., Uuemaa, E., Teimurian, T., Keesstra, S., Pham, T.D., Bui, D.T., 2019b. Multi-hazard exposure mapping using machine learning techniques: A case study from Iran. *Remote Sens.* 11, 1–20. <https://doi.org/10.3390/rs11161943>

Schweizer, J., Jamieson, J.B., 2003. Snowpack properties for snow profile analysis. *Cold Reg. Sci. Technol.* 37, 233–241. [https://doi.org/10.1016/S0165-232X\(03\)00067-3](https://doi.org/10.1016/S0165-232X(03)00067-3)

Selçuk, L., 2013. An avalanche hazard model for Bitlis Province, Turkey, using GIS based multicriteria decision analysis. *Turkish J. Earth Sci.* 22, 523–535. <https://doi.org/10.3906/yer-1201-10>

Suk, P., Klimánek, M., 2011. Creation of the snow avalanche susceptibility map of the krkonoše mountains using gis. *Acta Univ. Agric. Silv. Mendeliana Brun.* 59, 237–246. <https://doi.org/10.11118/actaun201159050237>

Swisstopo, 2021. https://shop.swisstopo.admin.ch/en/products/height_models/alti3D (20 December 2021)

Tiwari, A., G., A., Vishwakarma, B.D., 2021. Parameter importance assessment improves efficacy of machine learning methods for predicting snow avalanche sites in Leh-Manali Highway, India. *Sci. Total Environ.* 794, 148738. <https://doi.org/10.1016/j.scitotenv.2021.148738>

Varol, N., 2022. Avalanche susceptibility mapping with the use of frequency ratio, fuzzy and classical analytical hierarchy process for Uzungol area, Turkey. *Cold Reg. Sci. Technol.* 194, 103439. <https://doi.org/10.1016/j.coldregions.2021.103439>

Wang, Z., Liu, Q., Liu, Y., 2020. Mapping landslide susceptibility using machine learning algorithms and GIS: A case study in Shexian county, Anhui province, China. *Symmetry* (Basel). 12, 1–18. <https://doi.org/10.3390/sym12121954>

Winkler, K., Schmutlach, G., Degraeuwe, B., Techel, F., 2021. On the correlation between the forecast avalanche danger and avalanche risk taken by backcountry skiers in Switzerland. *Cold Reg. Sci. Technol.* 188, 103299. <https://doi.org/10.1016/j.coldregions.2021.103299>

SLF, 2021. Fatal avalanche accidents of the past 20 years, WSL Inst. Snow Avalanche Res. SLF. URL <https://www.slf.ch/en/avalanches/destructive-avalanches-and-avalanche-accidents/avalanche-accidents-of-the-past-20-years.html#tabellement1-tab2> (3 November 2021)

Yariyan, P., Avand, M., Abbaspour, R.A., Karami, M., Tiefenbacher, J.P., 2020. GIS-based spatial modeling of snow avalanches using four novel ensemble models. *Sci. Total Environ.* 745, 141008. <https://doi.org/10.1016/j.scitotenv.2020.141008>