

Refraction-aware integrated Georeferencing of bathymetric Laser Scanning Data

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Abstract

Bathymetric Laser Scanning (BLS) enables high-resolution mapping of underwater topography using green-wavelength laser pulses that penetrate the water column. However, precise georeferencing of the BLS data is affected by refraction at the air–water interface, which displaces submerged features and affects conventional strip adjustment methods. This paper introduces an integrated refraction-aware georeferencing workflow that combines refraction correction with trajectory and boresight optimization within a unified adjustment framework. Implemented using the scientific OPALS laser scanning software, the workflow starts with direct georeferencing of uncorrected laser returns, derives a water surface model, applies Snell's law-based refraction correction, and performs iterative strip adjustment until convergence. The approach was validated using UAV-borne topo-bathymetric LiDAR data from Lake Alm (Almsee) in Upper Austria, captured with a RIEGL VQ-840-GE sensor system. Comparative analysis across multiple processing scenarios demonstrates that the proposed integrated method significantly improves internal consistency between overlapping flight strips. The residual height discrepancies, quantified by the median absolute deviation (σ_{MAD}), were reduced from 4.5 cm using standard processing workflows to 2.1 cm with the integrated approach — an improvement exceeding 50%. A single processing pass was sufficient for the relatively calm conditions of the test site, though iterative refinement may benefit more dynamic water surfaces. The presented methodology is generic and can be embedded in any laser scanning framework supporting modular georeferencing and refraction correction.

1. Introduction

Bathymetric Laser Scanning (BLS) is an active multi-sensor measurement technique to capture 3D underwater topography using pulsed lasers operating in the green domain of the visible spectrum, typically 532 nm (Guenther et al., 2000). The emitted laser pulses travel through the atmosphere, partially reflect at the air–water interface, further propagate into the water column, and reflect a second time at the bottom of the water body or even multiple times if objects like vegetation are in the laser line of sight. At the water surface, the laser beam is deflected according to Snell's law of refraction and propagates with reduced velocity in water. Thus, refraction and runtime correction is a core component in the BLS processing chain.

The technology itself dates back to the 1960s, when it was first used in the military sector (Hickman and Hogg, 1969), followed by civil applications for near-shore nautical charting (Guenther, 1985) and coastal mapping (Wozencraft and Lillycrop, 2003). Around 2010, a new generation of topo-bathymetric LiDAR (Light Detection and Ranging) designed for simultaneous acquisition of topography and bathymetry was introduced (Fuchs and Tuell, 2010), and the application fields extended from the maritime area to inland waters (Pfennigbauer et al., 2011). Recently, sensor miniaturization and advances in carrier platform technology enabled the integration of relatively light weight bathymetry laser scanners onto Remotely Piloted Aerial Systems (RPAS), also called Uncrewed Aerial Vehicle (UAV) or drones (Kinzel and Legleiter, 2019; Mandlbürger et al., 2020). Regardless of the size and weight of the carrier platform and sensor, the BLS is always operated from the air, and data is collected along regular flight routes to ensure comprehensive coverage of the

bathymetry in shallow waters. For processing BLS data, this poses the challenge of dealing with both sensor orientation and laser ray refraction simultaneously.

Refraction correction of the raw bathymetric LiDAR observations is based on a digital representation of the continuous water surface. In case of still water surfaces like ponds and small- to medium-sized lakes, the water surface can be modeled with simple geometric primitives like horizontal or slightly tilted planes and can therefore be derived from auxiliary observation data (GNSS, total station, leveling device) with sufficient accuracy. For highly dynamic wavy water bodies, such as meandering rivers or wavy coastal areas, the air–water interface must be directly derived from the LiDAR data. To obtain reliable estimates of the instantaneous water surface, topo-bathymetric laser scanners employ a secondary infrared laser in addition to the water-penetrating green laser channel (Guenther et al., 2000) or sophisticated full waveform processing is applied to extract both the surface and the bottom from the complex return signal (Schwarz et al., 2019). If the water surface model is derived directly from the laser data, the extracted water surface returns must be georeferenced.

BLS sensors employ a Global Navigation Satellite System (GNSS) and an Inertial Measurement Unit (IMU) to position and orient the measurement platform. To obtain georeferenced coordinates of the laser returns, the scanner's measurements (range, beam deflection angle) are first transformed to 3D cartesian coordinates in the scanner's own coordinate system and then transformed to Cartesian Earth-Centered-Earth-Fixed (ECEF) coordinates based on the trajectory (i.e., direct georeferencing). Errors of the georeferenced laser points, which can be attributed to inaccuracies in the measurement data (GNSS, IMU, scanner) and the mounting calibration (lever

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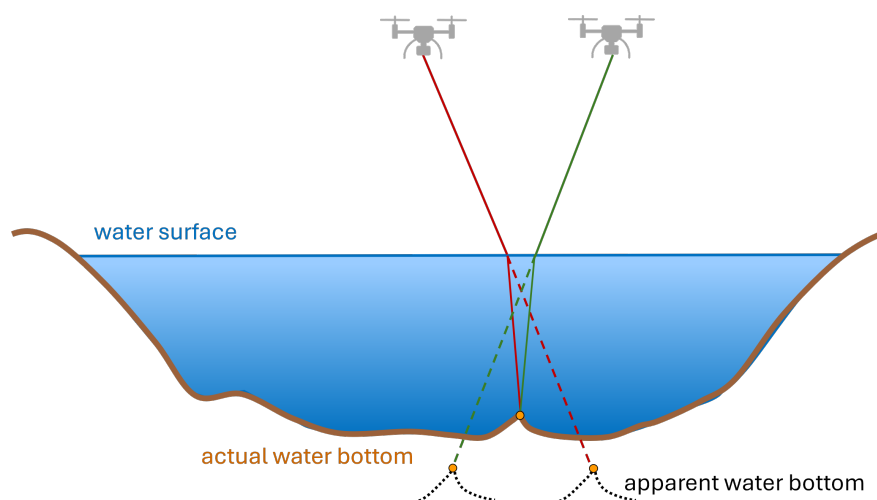


Figure 1. Schematic diagram of displacement of submerged features due to laser ray refraction at the air-water interface.

arms, boresight angles), are typically minimized by strip adjustment.

Various approaches have been presented in the literature for the adjustment of kinematic laser scan data, in particular for the compensation of residual errors of the trajectory and the sensor mounting and calibration. Glira et al. (2015) introduced an Airborne Laser Scanning (ALS) strip adjustment framework based on variants of the Iterative Closest Point (ICP) algorithm (Besl and McKay, 1992). The primary framework was further extended to compensate for time-dependent trajectory errors (Glira et al., 2016) and to integrate concurrently captured images in the adjustment (Jonassen et al., 2023). Brun et al. (2022) proposed a procedure to adjust flight trajectories based on 3D point-to-point correspondences between points of overlapping flight strips within a joint adjustment together with raw inertial and GNSS observations. A similar path of tightly coupling laser and inertial data and loose coupling of laser and GNSS data is introduced in Pöpl et al. (2024).

In all cited articles (Glira et al., 2015, 2016; Brun et al., 2022; Jonassen et al., 2023; Pöpl et al., 2024), corresponding features in overlapping flight lines are used as the basis for compensating or mitigating trajectory errors. The correspondences are established in the object space, i.e., an Earth-Centered-Earth-Fixed (ECEF) cartesian coordinate system. However, in BLS the correspondences are compromised by ray refraction at the air-water interface (Szafarczyk and Toś, 2023) as shown in Figure 1. In general, the coordinate differences of the corresponding features are minimized within the strip adjustment, and the unknown parameters (trajectory errors, boresight misalignment, lever arms, scanner calibration parameters) are estimated to mitigate the coordinate differences. If a large part of the acquired data is over dry land, e.g. for topo-bathymetric surveys of small inland waters such as rivers and ponds, the errors introduced when using uncorrected points are often negligible (Pöpl et al., 2024). However, if the underwater portion predominates, this deteriorates the estimation of the boresight angles, lever arms, and trajectory if refraction is not considered during georeferencing, leading to large discrepancies in the strip overlap area. In this case, refraction correction and strip adjustment must be performed simultaneously or at least coordinated. To the best of our knowledge, this is not described in the related literature so far.

We therefore propose a strategy to embed refraction correction in an integrated georeferencing approach and test the procedure with BLS data acquired at an Alpine lake in Upper Austria (Almsee). We describe the study site and the acquired BLS data in Section 2 and the proposed data processing pipeline in Section 3. In Section 4, we present the results followed by a critical discussion in Section 5. Section 6 concludes the article with a summary and outlook on future work.

2. Materials

To validate the proposed integrated georeferencing strategy, we conducted a UAV flight with a topo-bathymetric laser scanner system at Almsee, Upper Austria, in August 2025. The study site is shown in Figure 2. Almsee is a mountain lake in the Upper Austrian part of the Salzkammergut region. The outflow of Almsee is the Alm River, which drains into the Danube through the Traun River. With its largely natural shores, highly diverse vegetation belt and adjacent wetlands, this nutrient-poor lake provides habitats for many animal and plant species. It represents a relatively intact ecosystem and the area has been a protected nature reserve since 1965. The lake is located at an elevation of 589 m above sea level (ellipsoidal height: 634.5 m). The lake, which stretches from north to south, is 2.3 km long and has a maximum width of 700 m. Its surface area is approximately 85 hectares. The shallow lake exhibits a mean depth of around 3 m and features occasional sinkholes with a maximum depth of 9 m.

The entire lake was captured with a compact *RIEGL VQ-840-GE* airborne LiDAR system for combined topographic and bathymetric surveying (Riegl, 2025). The instrument weighs 10.3 kg including the integrated GNSS/IMU navigation device and was mounted on an Acecore Noa quadcopter UAV with a maximum take-off mass (MTOM) of 36.9 kg (cf. Figure 3). The laser scanner was operated from a flying altitude of 120 m above ground level (agl) with a flight speed of 8 m/s, a pulse repetition rate of 100 kHz and a beam divergence of 1 mrad. This results in a size of the laser footprint at the water surface of 12 cm and a single-strip median point density of 45 points/m². In total, the lake was captured with 4 flights and a total air time of 65 min. The entire flight mission consisted of 59 separate flight lines, which were jointly processed with the procedure outlined in the next section.

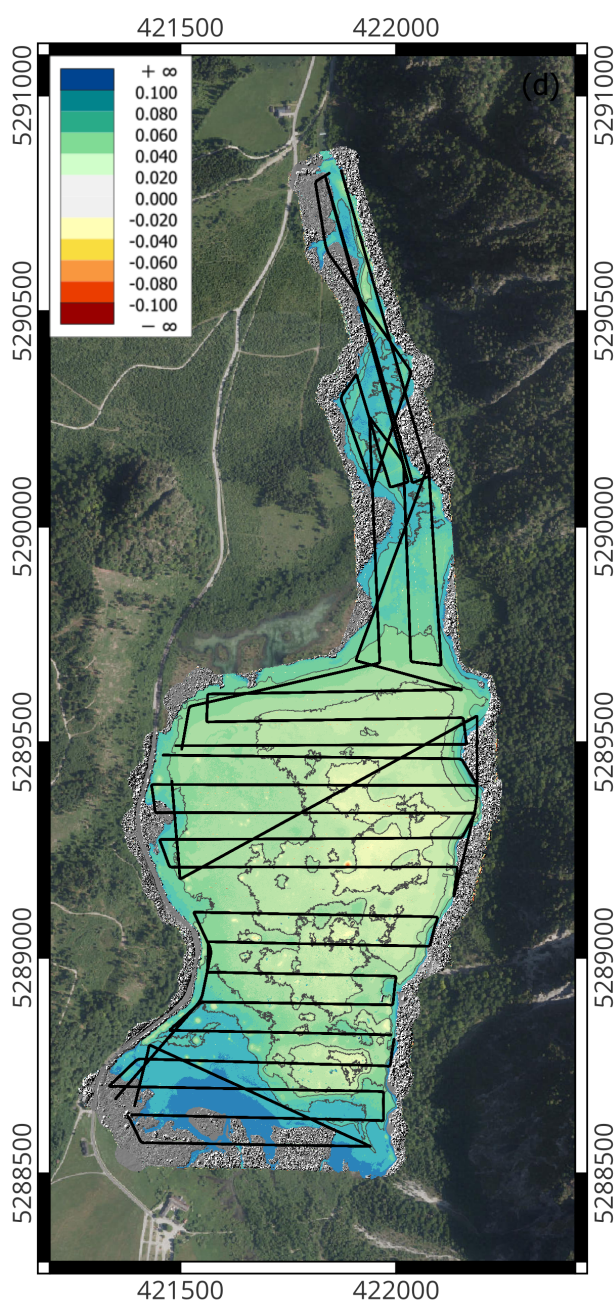


Figure 2. Study area Almsee, Upper Austria. Orthophoto map (basemap.at) superimposed with color coded water depth map and depth isolines. Map coordinate reference system: ETRS89/UTM 33 (EPSG:25833). WGS84 coordinates: $47^{\circ}45'N$, $13^{\circ}57'E$.



Figure 3. RIEGL VQ-840-GE topo-bathymetric laser scanner mounted on an Acecore Noa quadcopter UAV during data acquisition at Almsee in August 2025

3. Methods

Figure 4 shows the general workflow for integrated, refraction-aware georeferencing of BLS data. The processing pipeline consists of the following steps:

1. Initial trajectory estimation based on GNSS and IMU observations, e.g. via Kalman filtering
2. Direct georeferencing of the raw (i.e., uncorrected) laser returns
3. Derivation of a water surface model grid either from auxiliary measurements or from the raw georeferenced BLS point cloud
4. Refraction correction of the georeferenced laser returns
5. Optimization of trajectory and boresight alignment via strip adjustment
6. Error evaluation with focus on residual height discrepancies in overlapping flight areas
7. Repeat steps 3-6 until convergence

The method described is generic and can be integrated into any laser scanning software. In our case, we used the scientific laser scanning software OPALS (Pfeifer et al., 2014), which facilitates the implementation of the workflow due to its purely modular structure. In particular, we used the following OPALS modules (TU Wien, 2026):

- *DirectGeoref*: The module takes a time-stamped 3D laser point cloud stored in scanner coordinates (t, x, y, z), the flight trajectory in georeferenced coordinates (t , easting, northing, elevation, roll, pitch, yaw), and information about the mounting of the scanner system as input and returns the laser point cloud in the georeferenced coordinate system defined by the trajectory, i.e., ETRS89/UTM33 in our case. Note that both the trajectory and the laser points must be time-stamped and synchronized. Typically, GPS time (adjusted GPS time, GPS day seconds, GPS week seconds) is used as the common time system of both data streams. The module output is a data set stored in the OPALS Data Manager (ODM) file format (Otepka et al., 2012).

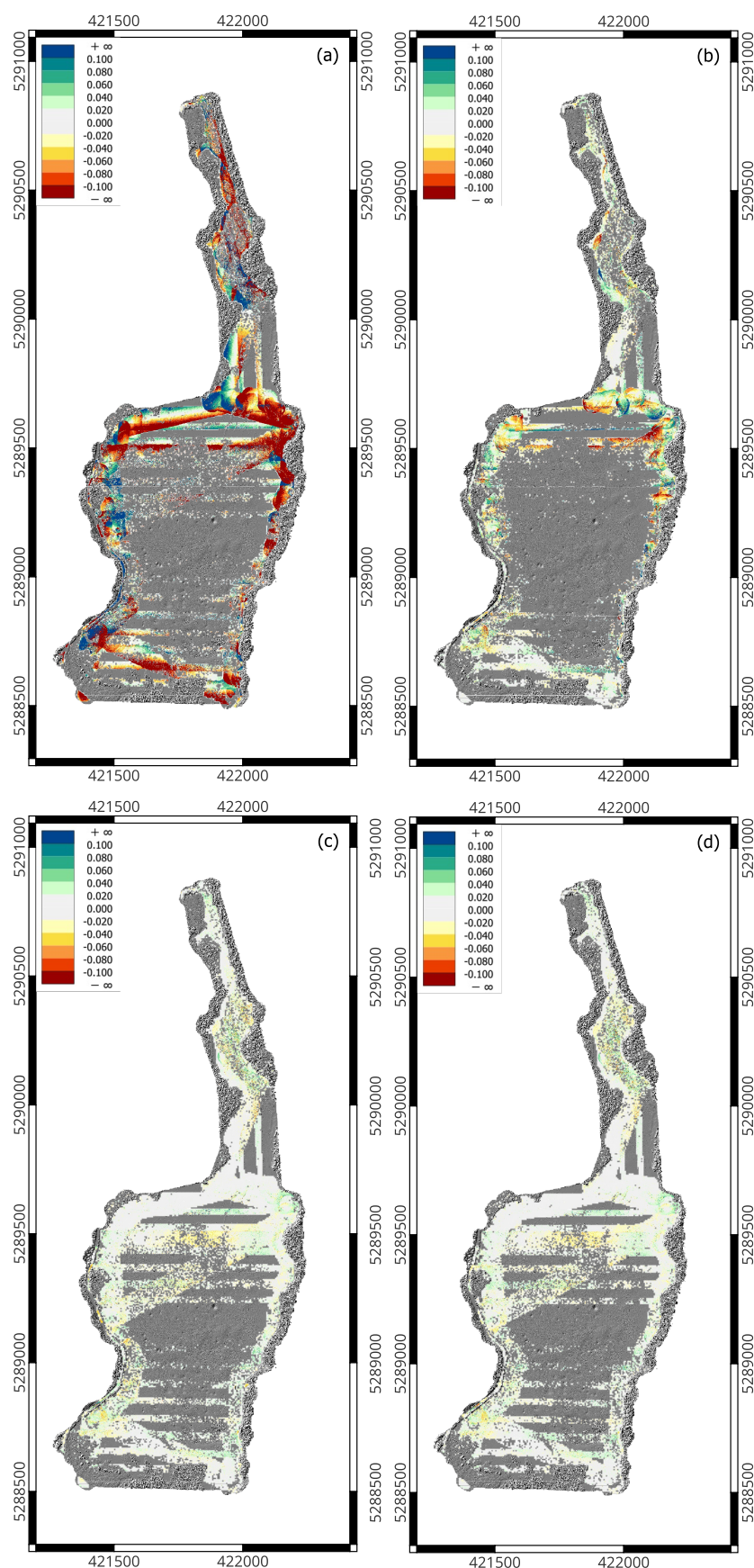


Figure 5. Results of integrated, refraction-aware georeferencing at study area Almsee, Upper Austria. color coded strip height differences (in m) in smooth surface areas; (a) direct georeferencing + refraction correction; (b) strip adjustment of uncorrected points + refraction correction after strip adjustment; (c) proposed workflow, single pass; (d) proposed workflow, double pass.

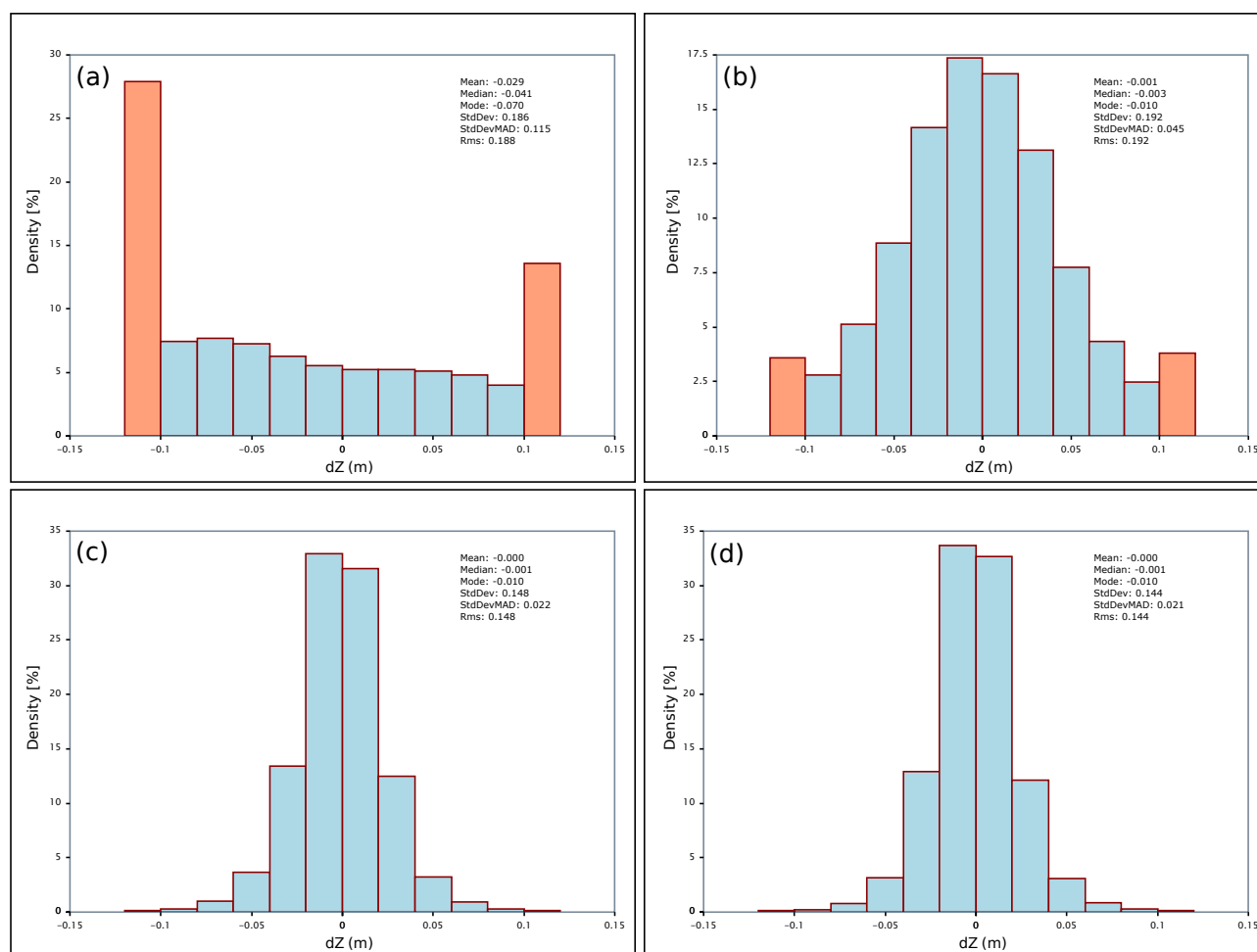


Figure 6. Histograms of the residual strip height differences for the four processing scenarios displayed in Figure 5; (a) direct georeferencing + refraction correction; (b) strip adjustment of uncorrected points + refraction correction after strip adjustment; (c) proposed workflow, single pass; (d) proposed workflow, double pass.

workflow shows lighter, improved results (less saturated colors), but still, remaining systematic deviations persist especially in the deeper parts of the lake where the effect of not considering refraction-induced errors is more pronounced. Using the proposed integrated workflow effectively reduces the residual height discrepancies in overlapping flight lines. This applies to both the single-pass (c) and double-pass (d) execution of the workflow. In both cases, the predominant whitish colors indicate deviations in the cm-range. The 2nd iteration (d) only marginally improves the results.

The strip difference histograms corresponding to the color-coded maps of Figure 5 are plotted in Figure 6. From (a) to (d) the distribution of the height differences gradually gets more centered around zero, with pronounced improvements when running the proposed method (c, d) compared to standard processing (a, b) and with only slight differences between the single-pass (c) and the double-pass (d) execution of the integrated workflow. σ_{MAD} improves from initially 11.5 cm for (a) and 4.5 cm for (b) to 2.1 cm for (c) and (d). Thus, the residual height deviations are reduced to 50% compared to the standard workflow (b).

Table 1 reports in detail the height difference distribution (centiles, deciles, quartiles). All reported metrics gradually improve from (a) to (d). In particular, the interquartile range (IQR:

Q75%-Q25%) improves from 4.5 cm for the standard laser data processing workflow (b) to 2.1 cm for the proposed integrated workflow (d). The same applies to the interdecile range (IDC: Q90%-Q10%) with an improvement from 9.8 (b) to 4.5 cm (d).

5. Discussions

The errors in scenario (a) (direct georeferencing) can be attributed to inaccuracies in the trajectory, as the steep topography surrounding the lake entails a suboptimal satellite configuration. The application of a standard BLS data processing workflow (b), which performs refraction and runtime correction only after strip adjustment and georeferencing (b), improves the results compared to (a), but the strip adjustment performs poorly as the corresponding submerged feature do not match properly. The geometric displacement scales with water depth, leading to smaller residual discrepancies in shallow water areas and larger deviations in deeper regions. This can be clearly seen when comparing the water depth map of Figure 2 with the color-coded height differences of Figure 5b. Smaller deviations occur in the southern part of the lake, where the lake is less than 1 m deep.

Although we proposed an iterative workflow, the second pass did not significantly improve the results. For the second pass, we re-calculated the water surface model and changed from

	Q1%	Q5%	Q10%	Q25%	Q50%	Q75%	Q90%	Q95%	Q99%
(a)	-0.294	-0.184	-0.142	-0.086	-0.024	0.043	0.104	0.144	0.245
(b)	-0.143	-0.073	-0.051	-0.023	-0.001	0.021	0.047	0.071	0.166
(c)	-0.067	-0.035	-0.024	-0.011	-0.000	0.010	0.023	0.034	0.068
(d)	-0.064	-0.033	-0.023	-0.011	-0.000	0.010	0.022	0.033	0.066

Table 1. Quantile statistics of strip height differences for processing scenarios a-d according to Figure 5. Units in (m)

an approximate description with a constant water level derived from averaged RTK-GNSS measurements to an explicit modeling of the water surface based on the laser returns. However, since the lake is almost level in the approximately 2 km range from its source to the outlet with a height difference of less than 15 cm, the effect of an improved water surface model in the second iteration did not have a large impact on the final results. This might change if the fluctuation of the water surface height is large, as is, for example, the case for mountain streams and even lowland rivers. However, for the Almsee data set, a single pass of the proposed integrated workflow was enough.

6. Conclusions

In this article, we introduced an integrated approach for georeferencing bathymetric laser scanning data. The approach starts with direct georeferencing of the raw laser returns based on an SBET trajectory and performs refraction and runtime correcting of the raw 3D point cloud based on a first approximate water surface model. Strip adjustment and fine georeferencing based on control points and patches is then performed with the refraction corrected point clouds, which overcomes potential feature matching problems, when using the uncorrected 3D points as input for strip adjustment. As the first pass uses approximate parameters (trajectory, mounting calibration, water surface model), the entire procedure can be repeated iteratively with gradually improved trajectories, system calibration, and water surface models, till convergence is reached.

The proposed method was evaluated with real-world data from a UAV-borne BLS data acquisition carried out at Almsee, Upper Austria in August 2025. Compared to standard BLS data processing, the residual height discrepancies could be reduced from 4.5 cm to 2.1 cm, which corresponds to an improvement of more than 50%. For the concrete Almsee data set, a single pass of the workflow proved to be sufficient, but iterations might become necessary for data sets with higher water surface height fluctuations.

The described workflow was implemented and tested based on the scientific laser scanning software OPALS, but is entirely generic and can, thus, also be integrated into other software packages including LiDAR data processing software suites of laser scanner manufacturers.

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