

## PERFORMANCE OF SITE VELOCITY PREDICTION IN SUNDALAND

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Commission 4, WG 7

**KEY WORDS:** Site Velocity, Plate Motion, Least Square Collocation, Crustal Deformation, Tectonic Geodesy

### ABSTRACT

Global Positioning System (GPS) technique has been extensively implemented in determination of crustal deformation globally. With the ability of providing solution up to millimeter (mm) level, this technique has proven to provide a precise estimate of site velocity that represents the actual motion of tectonic plate over a period. Therefore, this study aims to evaluate the site velocity estimation from GPS-derived daily position of station, respective to the global plate motion model and predicted site velocity via Least-Squares Collocation (LSC) method within the tectonically active region of Sundaland. The findings have indicated that stations with precise velocity estimates were consistent with global plate model and predicted velocity, with velocity residuals of 5 mm – 10 mm. However, stations that were severely impacted by continuous earthquake events such as in Sumatra were believed to be induced by the impact with consistently large velocity residuals up to 37 mm. Following the outcomes, this study has provided an insight on the post-seismic decay period plate motion which are induced by continuous tectonic activities respective to modelled plate motion.

### 1. INTRODUCTION

Global Positioning System (GPS) technique has frequently implemented in determination of geophysical events such as plate motion (Duman and Sanli, 2019). Observation from permanent GPS networks have proven to detect inter-plate and intra-plate deformation. Series of GPS observations combined with multiple geodetic techniques have also contributed to support the global plate motion model which are based on geophysical and geological data (Bastos et al., 2010) vice-versa whereby plate tectonic models can be biased by local effects and show inconsistencies while GPS observations depict motions over a short time interval, thus representing the present-day plate motion.

Therefore, this study intends to examine the efficiency of GPS-derived velocity, respective to the predicted velocities via global plate motion models. Site velocity prediction by Least-Squares Collocation (LSC) was also included to examine the capability of the model in velocity prediction. Within the tectonically active region such as Sundaland, observed velocity from GPS could differ from the predicted velocity by model as it is biased by local effects. Thus, the findings will give an insight towards the present-day plate motion respective to the modelled plate motion.

### 2. SEISMICITY OF THE SUNDALAND

The Sundaland plate region was regarded as a stable region (Hall, 2014) before the occurrences of major earthquakes along the Sumatra Subduction Zone (SSZ) and became a tectonically active region to this day. Holt et al. (1995) model indicated that the Sundaland has an eastward velocity respective to Eurasia at increasing southward from 10 mm/y to the north of South China to about 20 to 30 mm/y to the south (Holt et al., 1995; Chamot-Rooke et al., 1999). On the other hand, Geodynamics of South and South-East Asia project (GEODYSEA) GPS measurement showed that the Sundaland rotates clockwise around a pole of rotation located south of Australia, with an east to northeast

velocity increasing from 14 mm/y to the south to 23 mm/y to the north (Chamot-Rooke, 1999).

Four (4) major earthquakes with magnitude of >7.0Mw occurred on the western subduction zone of Sundaland from year 2004 until 2012 has resulted in a substantial impact towards the seismicity of the region of which it had disturbed the surrounding plate and triggered instability of the Sundaland. In a tectonically complicated region such as the Sundaland, series of earthquakes are thought to have increased lithosphere stress and raised seismic hazard over the region (Feng et al., 2015).

The 2004 Sumatra-Andaman earthquake that occurred on 26 December 2004 is considered as the largest earthquake that hits the region ever since. Erupting with a magnitude of 9.1Mw, it had severely impacted the Sumatra region as well as the western coast of Peninsular Malaysia. Consecutively, two earthquakes in the following years; 2005 Nias-Simuelue and 2007 Bengkulu earthquakes occurred within the same subduction zone, believed to be triggered by the 2004 earthquake (Feng et al., 2015; Aris, 2018) while the 2012 Indian Ocean earthquake, relatively occurred due to the stress transfer of the 2004 and 2005 earthquake (Gunawan et al., 2016).

These earthquakes also caused several tremors to be felt in Peninsular Malaysia (Aris, 2018) whereby series of moderate seismic activities by the Malaysia Meteorological Department (MMD) occurring in recent years such as tremors Bukit Tinggi and Jerantut, and sink holes around Batu Gajah and Ipoh are believed to be originated from these earthquakes (Aris, 2018). It is suspected that these tremors are resulting from the reactivation of major faults due to the impact of major earthquakes over the years.

### 3. METHODOLOGY

In quantifying the observed velocity and predicted velocity within the GPS CORS network in Sundaland, this study has been

phased into three stages. The first stage is determining the observed site velocity whereby GPS observation data will be processed using Bernese 5.2 high precision geodetic software in estimating GPS daily solution for selected MyRTKnet and SuGAR stations in Sumatra, Peninsular Malaysia and Northern Borneo area. Second stage is determining the predicted velocity through two (2) method; from plate motion model and LSC interpolation/extrapolation of velocity. Third stage will be the assessment on the performance of site velocity prediction, whereby the residuals between the observed and predicted velocity from the two methods will be analysed. Figure 1 shows the methodology implemented in this study.

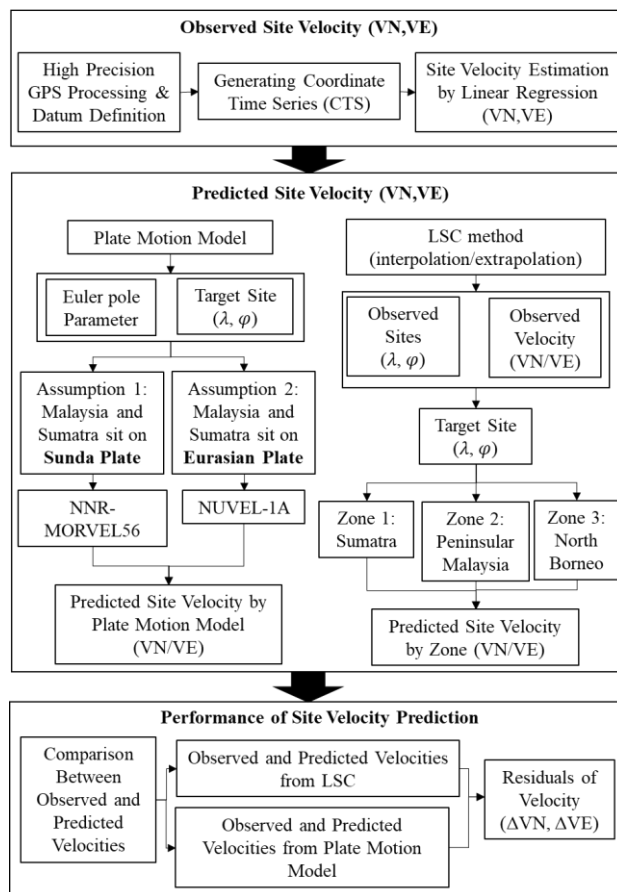


Figure 1. Methodology of the study.

### 3.1 GPS-Derived Site Velocity

Daily GPS solutions of year 2014 were constrained to International Terrestrial Reference Frame 2008 (ITRF2008) datum for selected MyRTKnet sites within Peninsular Malaysia and North Borneo region along with SuGAR sites within the region of Sumatra. From the processed daily GPS solutions, time series of the selected sites were plotted and fitted by linear regression model, following functional model shown in Equation 1.

$$y = at + b \quad (1)$$

where  $a$  and  $b$  are the coefficients to be estimated; velocity and initial position and  $t$  is the corresponding epochs. Following this equation, velocity of the site in Northing and Easting components were determined.

### 3.2 Predicted Site Velocity

This study implements two approach of site velocity prediction; via plate motion model and Least-Squares Collocation method. Predicting velocity from plate motion model requires the knowledge of the location of site in 3D Cartesian coordinates or geographical coordinates along with its Euler Pole parameters. Goudarzi et al., (2014) summarizes the Euler theorem for defining the velocity prediction, as follows:

$$\mathbf{v}_i^p = \mathbf{\Omega}^p \times \mathbf{x}_i = \begin{bmatrix} 0 & -\omega_z & \omega_y \\ \omega_z & 0 & -\omega_x \\ -\omega_y & \omega_x & 0 \end{bmatrix}^p \begin{bmatrix} x \\ y \\ z \end{bmatrix}_i \quad (2)$$

Whereby  $\mathbf{v}_i^p$  and  $\mathbf{x}_i(x_i, y_i, z_i)^T$  represent the velocity and the position of the station  $i$ , and  $\mathbf{\Omega}^p(\omega_x^p, \omega_y^p, \omega_z^p)$  represent the angular velocity or the Euler vector of the plate  $p$  associated with the station  $i$ . Following the Euler theorem, the site velocity were also predicted from two global plate motion model, namely the NNR-MORVEL56 (Argus et al., 2011) and NUVEL-1A (DeMets et al., 1994) by utilizing the UNAVCO Plate Motion Calculator.

Following the observed and predicted velocities from the two plate motion model, an approach of velocity prediction by LSC (Moritz, 1980) were also applied, with the knowledge of at least three (3) observed sites and one (1) predicted site. Equation 3 shows the functional model implemented.

$$S = C_{ST} C_L^{-1} L \quad (3)$$

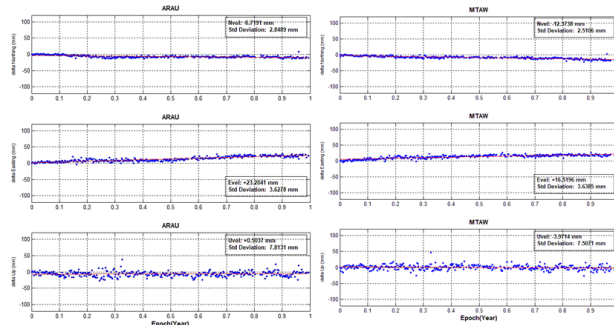
Whereby  $S$  is the predicted velocity.  $C_{ST}$  is empirical covariance functional matrix between signal  $T$  (i.e., intra-plate site velocity) at the observation points while  $C_L$  is the total covariance matrix of observation.

## 4. RESULTS AND ANALYSIS

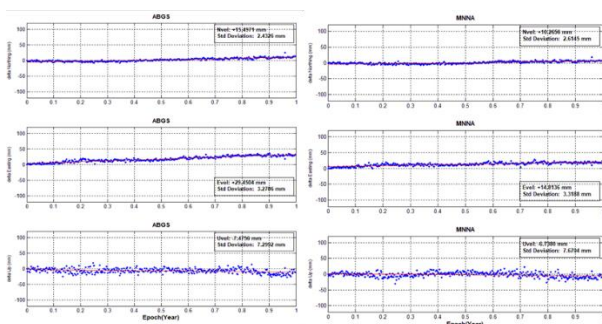
Several analyses were done towards the GPS-derived site velocity as well as the predicted velocity in understanding the depiction of the Sundaland motion. Thus, this section comprises of four parts: (1) GPS-derived site velocities of MyRTKnet and SuGAR sites, (2) Predicted velocities from plate motion model; NNR-MORVEL56 and NUVEL-1A. (3) Predicted velocities by Least-Squares Collocation method and (4) Analysis on the performance of the site velocity prediction.

### 4.1 GPS-Derived Site Velocities of MyRTKnet and SuGAR Sites

GPS Coordinate Time Series (CTS) for the selected MyRTKnet and SuGAR sites were plotted and velocity for each of the sites were estimated by applying Equation 1 into the time series. Figure 2 shows the time series plotted for MyRTKnet sites; ARAU in Peninsular Malaysia and MTAU in North Borneo while Figure 3 shows the time series plotted SuGAR sites; ABGS and MNNA in the Sumatra region. Estimated velocities for these sites are shown in Table 1.



**Figure 2.** GPS CTS of MyRTKnet sites; ARAU and MTAW.



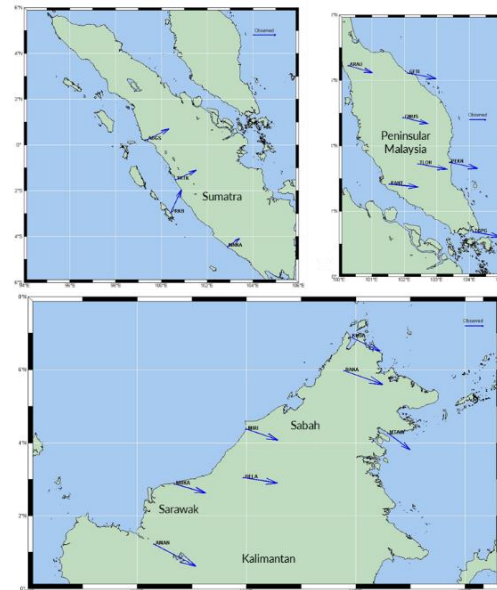
**Figure 3.** GPS CTS of MyRTKnet sites; ARAU and MTAW.

STATION	Observed Velocity	
	VN (mm)	VE (mm)
AMAN	-16.382	31.094
ARAU	-6.719	23.204
BANT	-2.615	28.082
BELA	-3.998	25.245
GETI	-5.334	27.077
GMUS	-5.856	24.001
KUDA	-10.303	21.910
MIRI	-7.917	23.092
MTAW	-12.374	16.520
MUKA	-6.765	23.157
PEKN	-5.663	26.915
RANA	-10.162	28.728
TGPG	-4.518	26.028
TLOH	-5.109	28.324
ABGS	15.497	29.450
MNNA	10.266	14.814
PRKB	28.350	13.601
TRTK	11.647	25.450

**Table 1.** Observed velocities at MyRTKnet and SuGAR sites.

Referring to Figure 2 and Table 1, MyRTKnet sites in shows and south-eastward trend of motion, dominantly towards east at an average velocity of 24 mm/year while SuGAR sites trends north-eastward motion at 21 mm/year (refer Figure 2 and Table 1). It can be observed that both of the sites are trending in linear motion within the post-seismic decay period after the last major earthquake that occurred in 2012. Figure 4 shows the

representation of observed velocity vector for both MyRTKnet and SuGAR sites.



**Figure 4.** Observed velocity vector plot of MyRTKnet and SuGAR sites.

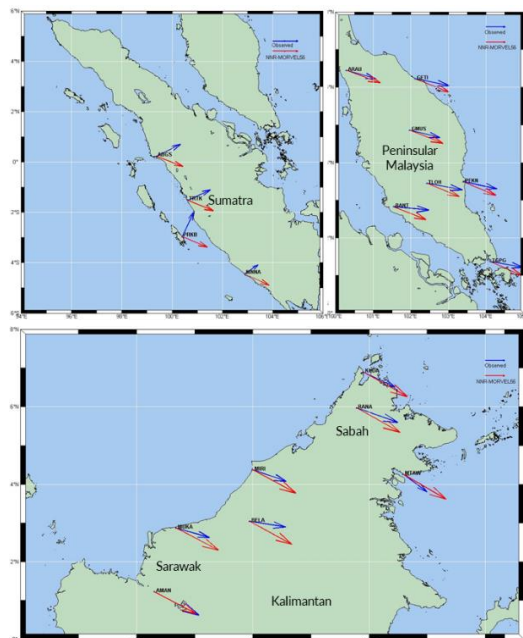
#### 4.2 Predicted Velocities from Plate Motion Model; NNR-MORVEL56 and NUVEL-1A

Following the determination of GPS-derived observed site velocities, velocity prediction was performed with the knowledge of the site locations along with its Euler pole parameters. Table 2 shows the predicted site velocity, deduced from two plate motion model; NNR-MORVEL56 and NUVEL-1A following the assumptions as shown in Figure 1.

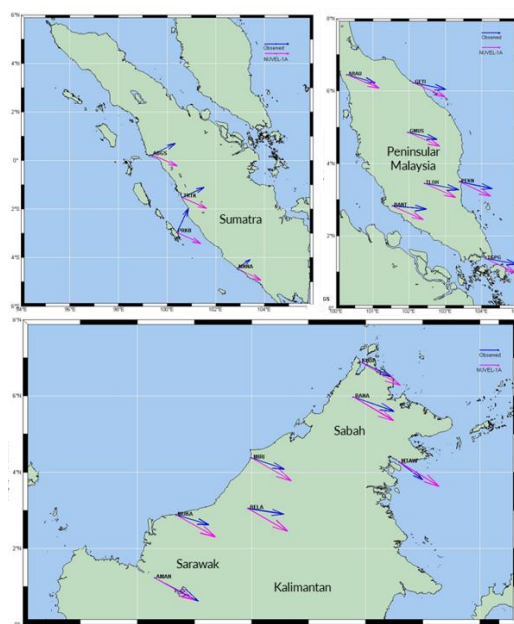
STATION	NNR-MORVEL56		NUVEL-1A	
	VN (mm)	VE (mm)	VN (mm)	VE (mm)
AMAN	-10.050	18.960	-11.410	20.360
ARAU	-7.360	20.200	-8.880	21.540
BANT	-7.680	19.380	-9.190	20.760
BELA	-10.590	19.320	-11.910	20.690
GETI	-7.820	20.130	-9.320	21.460
GMUS	-7.790	19.840	-9.290	21.190
KUDA	-11.210	19.980	-12.480	21.250
MIRI	-10.610	19.580	-11.930	20.920
MTAW	-11.430	19.500	-12.670	20.840
MUKA	-10.170	19.310	-11.530	20.670
PEKN	-8.140	19.510	-9.620	20.880
RANA	-11.180	19.830	-12.450	21.120
TGPG	-8.320	19.020	-9.790	20.420
TLOH	-7.900	19.510	-9.400	20.890
ABGS	-7.130	18.750	-8.670	20.160
MNNA	-8.020	17.540	-9.510	19.010
PRKB	-7.390	17.920	-8.910	19.370
TRTK	-7.450	18.300	-8.970	19.740

**Table 2.** NNR-MORVEL56 and NUVEL-1A predicted velocity

Referring to Table 2, predicted velocities between NNR-MORVEL56 and NUVEL-1A for MyRTKnet and SuGAR sites shows a trend of south-eastward motion at an average of 20 mm/year. Slight difference of velocity estimates between the two plate motions model were believed due to different definition of Euler pole parameters between the model. Figure 5 shows the predicted velocity vector plot for NNR-MORVEL56 with respect to the GPS-derived observed velocity while Figure 6 shows the predicted velocity vector plot for NUVEL-1A model, respective to the GPS-derived observed velocity.



**Figure 5.** Predicted NNR-MORVEL56 velocity with observed velocity vector plot of MyRTKnet and SuGAR sites.



**Figure 6.** Predicted NUVEL-1A velocity with observed velocity vector plot of MyRTKnet and SuGAR sites.

### 4.3 Predicted Velocities by Least-Squares Collocation Method

Following the prediction of velocity from the two plate motion model; NNR-MORVEL56 and NUVEL-1A, an approach of velocity prediction by implementing Least-Squares Collocation (LSC) method was performed to examine the capability of this model for velocity prediction. Referring to Figure 1, the velocity prediction by LSC approach was performed according to three zones; Sumatra, Peninsular Malaysia and North Borneo. Within each of these zones, several sites were treated as target sites whereby the velocity of these sites will be predicted with the knowledge of three (3) neighbouring sites. Table 3 shows the predicted velocities of the selected target sites by implementing LSC. Discussion on the LSC-predicted velocity will be in the next section.

STATION	Predicted LSC Velocity	
	VN (mm)	VE (mm)
TLOH	-4.719	27.763
RANA	-11.367	31.383
TRTK	24.798	14.222
PEKN	-1.913	13.871
BANT	-3.259	15.202
ARAU	3.401	30.413
BELA	-3.919	10.545

**Table 3.** LSC- predicted velocity for MyRTKnet sites and SuGAR sites.

### 4.4 Analysis on Performance of Site Velocity Prediction

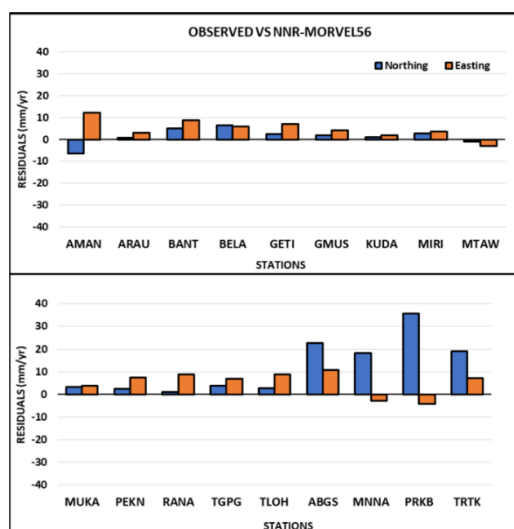
GPS-derived site velocity followed by predicted velocity from the plate motion model and LSC method were analysed through residuals between observed velocity and predicted velocity from the two different models, defined by the residuals of the velocity that has been determined. Table 4 shows the residuals between GPS-derived observed velocities and predicted velocities from NNR-MORVEL56 and NUVEL-1A plate motion model

STATION	Residuals (Observed Velocity vs NNR- MORVEL56)		Residuals (Observed Velocity vs NUVEL-1A)	
	VN (mm)	VE (mm)	VN (mm)	VE (mm)
AMAN	-6.332	12.134	-4.972	10.734
ARAU	0.641	3.004	2.161	1.664
BANT	5.065	8.702	6.575	7.322
BELA	6.592	5.925	7.912	4.555
GETI	2.486	6.947	3.986	5.617
GMUS	1.934	4.161	3.434	2.811
KUDA	0.907	1.930	2.177	0.660
MIRI	2.693	3.512	4.013	2.172
MTAW	-0.944	-2.980	0.296	-4.320
MUKA	3.405	3.847	4.765	2.487
PEKN	2.477	7.405	3.957	6.035
RANA	1.018	8.898	2.288	7.608
TGPG	3.802	7.008	5.272	5.608
TLOH	2.791	8.814	4.291	7.434
ABGS	22.627	10.700	24.167	9.290
MNNA	18.286	-2.726	19.776	-4.196

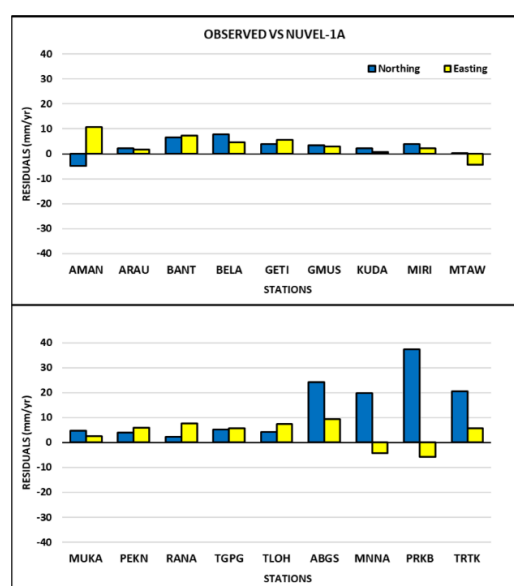
PRKB	35.740	-4.319	37.260	-5.769
TRTK	-6.653	32.900	-8.093	34.420

**Table 4.** Residuals between GPS-derived velocities and predicted velocities from NNR-MORVEL56 and NUVEL-1A plate motion model.

Referring to Table 4, The residuals between the observed and predicted velocity from both NNR-MORVEL56 (Figure 7) and NUVEL-1A (Figure 8) for MyRTKnet sites shown a relatively small residuals averaging at 5-10 mm, while SuGAR sites shown significantly large residuals, up to 37mm. It is suspected that SuGAR sites within the Sumatra region are largely influenced by local effect; continuous impact of earthquakes within the Sumatra Subduction Zone. Despite showing small residuals between observed and predicted velocities from the plate motion model, both MyRTKnet sites and SuGAR sites were still induced by the effects of the major earthquakes within the post-seismic decay period.



**Figure 7.** Residual plot between GPS-derived velocities and NNR-MORVEL56 plate motion model.

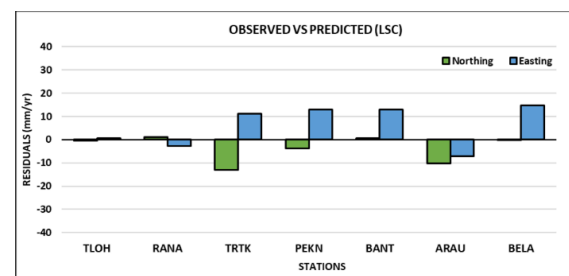


**Figure 8.** Residual plot between GPS-derived velocities and NUVEL-1A plate motion model.

Following the residuals between the observed and predicted from the plate motion model, the residuals between GPS-derived velocity and predicted velocity by LSC approach for selected MyRTKnet and SuGAR sites was also determined. Table 5 shows residuals between GPS-derived observed velocities and predicted velocities via LSC Figure 9 shows the residual plot between the GPS-derived velocity and predicted velocity via LSC approach.

STATION	Residuals (Observed Velocity VS LSC-Predicted)	
	VN (mm)	VE (mm)
TLOH	-0.389	0.561
RANA	1.204	-2.655
TRTK	-13.151	11.228
PEKN	-3.750	13.044
BANT	0.644	12.879
ARAU	-10.120	-7.209
BELA	-0.079	14.700

**Table 5.** Residuals between GPS-derived velocities and predicted velocities via LSC.



**Figure 9.** Residual plot between GPS-derived velocities and LSC-predicted velocities

On the contrary, predicted velocities of the residuals between the predicted site velocities by LSC at known points in Peninsular Malaysia, North Borneo and Sumatra are relatively small averaging between 0.5mm up to 15mm. Referring to Table 9, MyRTKnet sites; TLOH and RANA shown a small residual between 0.5-2.6 mm while SuGAR sites shows average residual of 12 mm, lower compared to predicted velocity from the plate motion model. Small residuals between the GPS-derived velocity and the LSC-predicted velocity have shown efficiency of the model to be implemented for velocity prediction.

## 5. CONCLUSION

The observed velocity of MyRTKnet shows a trend of north-eastward motion at an average of 24 mm/year while both NNR-MORVEL56 and NUVEL-1A velocity prediction shows that the sites are trending south-east motion at an average of 20 mm/year. Slight difference of velocity estimates between the two plate motions model were believed due to different definition of Euler pole parameters between the model.

The residuals between the observed and predicted velocity from both NNR-MORVEL56 and NUVEL-1A for MyRTKnet sites are relatively small, averaging at 5-10 mm while SuGAR sites shown large residuals, up to 37 mm, indicating the local effect bias in the observation. Meanwhile, residuals between the predicted site velocities by LSC at selected sites in Peninsular Malaysia, North Borneo and Sumatra are relatively small averaging between 0.5mm up to 15mm, thus indicating that the model is efficient in predicting velocities.



However, velocity prediction by LSC can be optimized with larger number of observed sites along with enhanced geometry through grid network development between the observed sites and predicted sites.

## ACKNOWLEDGEMENT

The authors would like to thank the Ministry of Higher Education (MOHE) Malaysia for providing the funds through the Fundamental Research Grant FRGS/1/2019/TK04/UTM/02/4 (Vot R.J130000.7851.5F209) which has contributed to the vital findings of this study.

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